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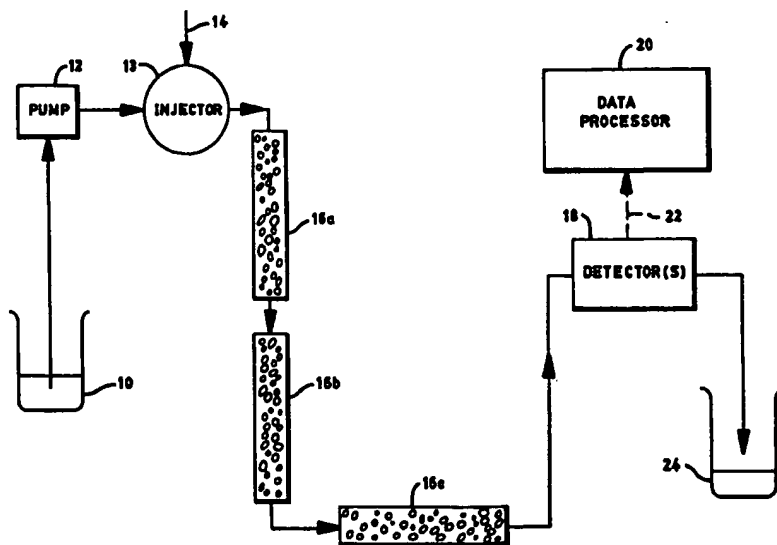
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(57) Abstract

A system and method for analyzing data from a gel permeation chromatography (GPC) or size exclusion chromatography (SEC) system for determining a polymeric sample's molecular weight distribution (MWD) and intrinsic viscosity law (IVL). Data from two or more detectors is used with a least-squares minimization fit. A novel method includes the simultaneous determination of a sample's MWD and IVL using data from two or more detectors. Detectors include a Light Scattering (LS) detector, viscometer (V) and a refractive index (RI) detector. The present invention is insensitive to detector noise in the baseline regions of the peak curve.

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SYSTEM AND METHOD FOR DETERMINING MOLECULAR WEIGHT
AND INTRINSIC VISCOSITY OF A POLYMERIC DISTRIBUTION
USING GEL PERMEATION CHROMATOGRAPHY

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FIELD OF THE INVENTION

The present invention relates to analysis of data from gel permeation chromatography (GPC) instrumentation, and more particularly to a computer system and method for analyzing data to determine absolute molecular weight and intrinsic
10 viscosity.

BACKGROUND OF THE INVENTION

The molecular structure of a synthetic polymer determines its end-use and its process characteristics, such as hardness, tensile strength, drawability, elastic modulus,
15 and melt viscosity. The most important determinants that define the molecular structure of synthetic polymers are the chemical nature of their repeating units, their molecular weight distribution (MWD), and their molecular topology (branching).

The separation of a polymer sample by gel permeation chromatography (GPC) followed by detection allows one to determine the molecular weight distribution
20 (MWD) and the intrinsic viscosity law (IVL) of a polymeric sample. The IVL can reveal the branching properties of a sample. Another term used for GPC is size exclusion chromatography (SEC).

In a GPC separation, a molecule's effective size, not its molecular weight *per se*, determines its elution volume. For example, two polymers may have the same
25 molecular weight, but may differ in composition or branch topology. Such differences can lead to different elution volumes. Thus, elution volume by itself determines a sample's molecular weight distribution in a relative, not an absolute sense.

Following separation, one or more detectors record the physical properties of the eluent stream. It is the mathematical analysis of these data from which the MWD
30 and IVL of the sample can be obtained.

When narrow standards of known molecular weight (MW), the sum of atomic weights of all atoms in a molecule, are available, and these standards are of the same polymeric material as the sample, molecular weight calibration is straightforward to perform. Injections of the narrow standards determine the chromatography column set's
35 MW calibration curve (log MW versus elution volume). Under these circumstances,

only a single concentration detector (such as a refractive index (RI) detector) is needed to determine the MWD.

If no such standards are available, dual detection schemes can be employed to determine the sample's MWD. A first typical dual detection system employs refractive index (RI) and light scattering (LS) detection. A second known system employs RI and viscometric (V) detection. The data from both such systems can be used to determine a sample's MWD.

The RI-V detection system allows the additional determination of the molecular topology of the polymer through a plot of its intrinsic viscosity law (IVL). The IVL of a sample is its intrinsic viscosity as a function of its molecular weight. The intrinsic viscosity is the ratio of the sample's specific viscosity (measured by the viscometer) to its concentration (measured by the concentration detector).

In the case of RI-V detection, polymer calibration standards are needed to determine the MWD and IVL, but the repeat units do not need to have the same chemical nature as those of the polymer sample. The RI-LS detection strategy requires no additional calibration standards.

For both systems, the RI detector is used to measure a peak's concentration profile. In place of an RI detector, a suitably calibrated UV/Vis absorbance detector, evaporative light scattering detector (EVS), or infrared (IR) detector may be substituted to perform the same function.

The LS and V detectors are commonly referred to as "molecular-weight sensitive" detectors. Such detectors respond to the product of the sample's concentration and its molecular weight raised to some power.

A combination of a concentration detector and a molecular-weight-sensitive detector greatly increases the information content available from a typical analysis. But the increase in the available information expands the complexity of data analysis. For both systems, algorithmic methods are required to analyze the detector responses in order to obtain the sample's MWD. In the RI-V system, an additional algorithmic method is needed to determine the sample's IVL.

The accuracy and the precision of the MWD and the IVL depend not only on the quality of the data obtained from the respective chromatographic systems, but also on the details of the data analysis methodology. Thus, data analysis methods become an essential element in the GPC analysis of polymers.

At evenly spaced time intervals, each detector records a measurement of the properties of the separated sample as it elutes from the column and passes through a detector's flow cell. Each measurement, averaged over a narrow time range, corresponds to a narrow range in the sample's molecular weight distribution. The
5 molecular weight range corresponding to a measurement recorded at a single time interval is referred to as a "slice".

A slice can be referenced by its slice number, its elution time, or its elution volume. Typically, elution volume is obtained by multiplying the elution time of a slice by the nominal flow rate of the pump. A particular slice is typically referred to by
10 its slice number or elution volume, with no loss of generality.

The RI, LS, and V detectors are used to measure, respectively, the concentration c_i , the Rayleigh ratio R_i , and the specific viscosity sp,i , for each slice i .

If a pair of chromatographic profiles are obtained from two detectors, the ratio of the respective responses can be formed to obtain useful quantities. For example, if c_i
15 and R_i are the measurements of concentration and the Rayleigh ratio from the i th slice, the ratio $i = R_i/c_i$ is proportional to the molecular weight of that slice. If c_i and sp,i are the slice measurements of concentration and specific viscosity, the ratio $[i = sp,i / c_i$ equals the intrinsic viscosity of the slice.

Both the MWD and IVL need to be measured over the whole peak region.
20 Typically, this is accomplished by fitting a smooth parameterized model to these ratios as a function of slice number or elution volume. The logarithm of the ratios, $\log(R_i/c_i)$ and $\log(sp,i / c_i)$, both tend to be nearly linear functions of elution volume, so low-order polynomials as a function of elution volume are typically fit to these quantities.

A major problem is that the noise present in the detector responses introduces
25 errors in the quantities computed from slice measurements. Each of the known detectors employed for GPC contains non-idealities in their responses. Typically, these non-idealities fall into two categories, baseline drift and stochastic detector noise. Detector noise can also be referred to as system noise. Baseline drift in a thermally stabilized chromatograph is accurately compensated for by baseline correction
30 procedures.

Detector noise is an irreducible component of the measurement process. The origin of this noise, seen as fluctuations in the baseline, is the result of several fundamental phenomena. One is the shot noise of the light sources such as in RI and LS detectors. Other origins are thermal noises associated with amplifiers in all

detectors; fluctuations in the pump flow rate; and thermal variations. Particulate, contaminants, and bubbles can also add additional noise components to the signal.

The net result of these effects is manifested in stochastic noise added to each slice measurement. Such additive noise has zero mean and a well-defined standard deviation. The standard deviation of the noise will in general be different for the different detectors, but each detector's noise is constant throughout the separation.

The effect of the detector-noise-induced error in the slice-measurements is to introduce error in the quantities $\log(Ri/ci)$ and $\log(sp,i /ci)$. Because ci is in the denominator, the noise in these quantities increases as the response in the concentration profile decreases. Because of the logarithm, the noise in these quantities also increases as the response of the molecular-weight-sensitive detector decreases. Thus, the noise in $\log(Ri/ci)$ and $\log(sp,i /ci)$ increases dramatically in the tails (leading and trailing edges) of a chromatographic peak.

Further, near the peak tails, the noise in the responses can cause the ratios to have negative values. The logarithm of a negative number is not defined. Eliminating such slice data will bias the results. This issue of dealing with the logarithm of the response ratios is well described in the recent paper "Systematic Deviations due to Random Noise Levels in Size Exclusion Chromatography Coupled With Multi Angle Laser Light Scattering" by P. Tackx and F. Fosscher, 1997, *Anal. Comm.* 34, 295-297.

The question remains as to how to fit a smooth model curve to $\log(Ri/ci)$ and $\log(sp,i /ci)$ across a complete peak profile given the presence of detector noise.

Prior to the present invention, it was assumed that in the peak tails, the quantities $\log(Ri/ci)$ and $\log(sp,i /ci)$, because they appeared dominated by noise, contained no useful information. Least-squares fitting of models were then confined to the "heart" of the peaks where the ratios' signal-to-noise ratio (SNR) were high. Users were required to manually decide the demarcation between the region to which the model is fit, and regions to exclude from the model fit.

However, to determine the MWD and IVL throughout the peak, the values of these quantities were nevertheless needed in the peak tails. The prior practice was to extrapolate the model results to the peak tails. The results obtained from such extrapolations are notoriously sensitive to the choice of the fitting region and the extrapolation method, as Tackx and Fosscher point out.

SUMMARY OF THE INVENTION

The present invention provides an accurate data analysis method that can be applied to the data acquired from detectors for determining a polymeric sample's molecular weight distribution (MWD) and intrinsic viscosity law (IVL).

According to the invention, a pair of chromatographic profiles is obtained from two detectors, and one set of responses is compared to a model that is a function of another set of responses. For example, if c_i and R_i are the measurements of concentration and the Rayleigh ratio for the i th slice, the quantity R_i is compared to a model of R_i obtained from c_i . If c_i and sp,i are the measurements of concentration and the specific viscosity from the i th slice, the quantity sp,i is compared to a model of sp,i obtained from c_i . This method then eliminates the need to take the ratio of profiles and the logarithm of these ratios and thereby allows the use of slice measurements made throughout a peak profile, including the regions in the peak tails.

In a first embodiment of the invention, an accurate method for determination of MWD and IV of polymeric samples using the technique of GPC or SEC separations and two or more detectors is provided.

A first implementation of the first embodiment of the present invention includes a method of using least-squares minimization that takes a first detector signal, constructs an initial model curve using a parameterized model curve which describes sample properties. Least-squares minimization is then performed on the initial model curve and a second detector signal to produce a best fit model curve and parameters.

A second implementation of the first embodiment includes a method for determining a sample's molecular weight calibration curve using two or more detectors. Data from a concentration detector is processed into slices, and an initial model curve using a parameterized model curve describing $\log M$ (log molecular weight) versus elution volume is generated. This initial model curve is used to describe the Rayleigh ratio of the slices from the concentration detector. Second data from a Light Scattering (LS) detector is processed into the Rayleigh ratios of the slices. Least-squares minimization is then performed on the initial model curve and the Rayleigh ratios of the slices from the second detector data, resulting in a best fit model curve and parameters. The sample's molecular weight distribution (MWD) is then calculated.

A third implementation of the first embodiment of the present invention includes a method for determining a sample's intrinsic viscosity versus elution volume using two or more detectors. Data from a concentration detector is processed into slices, and an initial model curve using a parameterized model curve describing $\log [\eta]$

versus elution volume is generated. This initial model curve describes the specific viscosity of the slices from the concentration detector. Second data from a viscometer (V) detector is processed into the specific viscosities of the slices. Least-squares minimization is then performed on the initial model curve and specific viscosity of
5 slices from the second detector data, resulting in a best fit model curve describing $\log [\eta]$ versus elution volume.

In a second embodiment of the present invention, the simultaneous determination of a sample's MWD and IVL using data from two or more detectors is performed. Data from a concentration detector is processed into slices. An initial
10 model curve is constructed using this data, using a parameterized model curve describing $\log [\eta]$ versus $\log M$ for the sample, and using the hydrodynamic volume of slices from a universal calibration curve. This initial model curve describes the specific viscosity of the slices as a function of the concentration detector responses. Second data from a viscometer (V) detector is processed into the specific viscosities of the
15 respective slices. Least-squares minimization is then performed on the initial model curve, and specific viscosity of respective slices from the second detector data, resulting in a best fit model curve describing $\log [\eta]$ versus $\log M$. From this best fit model curve, the IVL and MWD are determined.

A third embodiment of the present invention includes a reformulation of a least
20 squares minimization fit to eliminate the use of ratios and logarithms, thereby allowing the fit to include all the data throughout a peak.

A fourth embodiment of the present invention includes using weighted least-squares minimization fit where noise in compared quantities varies throughout the whole of the peak region, whereby the least-squares fit then can be carried out over the
25 whole of the peak region.

An advantage of the present invention is that it allows the inclusion of regions that contain no signal; e.g., baseline responses that fluctuate about zero from either, or both, detectors. Another advantage of the present invention is the improved accuracy and precision of the sample's MWD, as determined by the two systems under
30 consideration. Further, the least-squares problem is formulated to avoid taking ratios or logarithms of ratios of noisy data. Also, the present invention is considerably less sensitive to measurement errors, especially in the tails of the peaks. The present invention provides improved accuracy and precision of the IVL for the second embodiment.

Still another advantage of the present invention is that the IV law and molecular weight calibration are estimated from a single fit to all the slice data. The need to perform multiple fits and extrapolations is avoided, as are systematic errors that result from performing additional fits.

5

BRIEF DESCRIPTION OF THE DRAWING

The foregoing and other features and advantages of the present invention will be more fully understood from the following detailed description of illustrative embodiments, taken in conjunction with the accompanying drawings in which:

10 Fig. 1 is an overview of a Gel Permeation Chromatography system which provides data to be analyzed by a system including the present invention;

Fig. 2 is an illustrative computer system for analyzing data according to the present invention;

15 Fig. 3 is a graph of a simulated MWD of a sample, given a mass injected on column, normalized to give $dm/d\log M$, the mass per unit logarithmic interval of MW;

Fig. 4 is a graph showing plots of three intrinsic viscosity laws;

Fig. 5 is a sample molecular weight calibration curve;

Fig. 6 is a graph showing sample concentration versus elution volume;

20 Fig. 7 illustrates the detector profiles based on the instrumental responses to the concentration profile described in Fig. 6;

Fig. 8 illustrates the detector responses of Fig. 7 with the inclusion of detector noise;

Fig. 9 illustrates the molecular weight calibration curve obtained from the slice data versus elution volume;

25 Fig. 10 illustrates the molecular weight calibration obtained from the illustrative embodiment as compared with a prior art method;

Fig. 11 displays the sample's IV law determined from RI-V detection according to the illustrative embodiment as compared to a prior art method;

30 Fig. 12 is an overview of the steps performed according to one embodiment of the present invention;

Fig. 13 is an overview of the steps performed for estimating a sample's molecular weight distribution (MWD) from RI-LS detection in accordance with the embodiment of Fig. 12;

Fig. 14 is an overview of the steps performed for estimating a sample's intrinsic viscosity versus elution volume from RI-V detection in accordance with the embodiment of Fig. 12;

Fig. 15 is an overview of the steps performed according to another embodiment for estimating a sample's intrinsic viscosity law and molecular weight distribution from RI-V detection according to the present invention; and

Fig. 16 is an overview of the least-squares fit step utilized by the embodiments shown in Figs. 12-15.

10 DETAILED DESCRIPTION

An illustrative gel permeation chromatography (GPC) system for analyzing molecular weight distributions according to the present invention is illustrated in Fig. 1. A solvent reservoir 10 provides solvent which is pumped by a solvent pump 12. At the injection valve 13, the polymeric sample 14 is introduced into the solvent flow. The solvent along with the polymeric sample 14 then passes through a set of columns 16 which contain the chromatographic bed. The solvent then passes through a detector 18, where one or several detectors analyze the solution and determine the presence and properties of polymer chains. This information is supplied to a data processor 20, as shown by arrow 22. The waste solution then collects in a container 24.

20 The GPC columns 16 contain packed beads (the chromatographic bed) that possess a distribution of pore sizes. An illustrative embodiment of such a system is a Waters 150CV+ GPC Viscometry Chromatography System, and Styragel Columns, both manufactured by Waters Corporation, 34 Maple Street Milford, MA, 01757.

Injection of the sample 14 into the flowing stream forces it through the column set 16. The separation is effected by a sieving mechanism. The pores exclude the larger molecules and retain the smaller molecules. Larger molecules see a column set having a relatively small effective volume. Smaller molecules see a column set having a relatively large effective volume. Consequently, the larger molecules elute first, and the smaller molecules elute later. The detectors 18 follow the column set 16 and measure the physical properties of the eluent.

30 The data processor 20 Fig. 2 includes a database 26 and a processor 28. The database 26 includes long-term storage such as magnetic disks, tapes and opto-magnetic discs. The database 26 in this illustrative embodiment is a relational database. The processor 28 accesses the data stored in database 26 for processing and producing

information which may be stored back in the database 26, or displayed on a workstation 30, or printed out (not shown). The data processor 20 can also include instrumentation to process and convert the data 22, including A/D (analog to digital) conversion circuits, sample and holds, and other devices (not shown).

5 In the illustrative embodiment, the data processor is a general purpose computer, such as an Intel Pentium® based personal computer running Microsoft Windows® 95 or Windows NT. The processing application software is Millennium³²® as produced by Waters Corporation of Milford, MA. Millennium³² is a chromatography information and systems manager that allows a chromatographer to
10 control instrumentation, and to acquire, store and retrieve data obtained from detectors. It also allows the chromatographer to process that data and store, retrieve display, and print the processed results in graphical and tabular form.

The Millennium³² software product includes several components. One software component controls instrumentation (the pump 12, the autoinjector 13,
15 and the detectors 18) and acquires data (primarily from the detectors). Another component is the database 26 which is an Oracle database that stores and serves up information.

Another component is the application software that processes and extracts information from the data and presents it in reports. A report generator allows the user
20 to create, manage and print reports. A graphical user interface (GUI) allows the user to interact with all these subsystems and components from the monitor 30. The illustrative embodiment of the present invention is implemented within the data processing component of Millennium³².

Two categories of detectors can provide signal inputs 22 to Millennium³². One
25 category comprises detectors manufactured by Waters, the other contains third party detectors. The output from Water's detectors communicate via an IEEE-488 interface (IEEE-488 is the IEEE Standard Digital Interface for Programmable Instrumentation, ANSI/IEEE Standard 488-1978). The signal from the detector is in analog form on the IEEE-488 cable. The IEEE-488 cable connects to Millennium³² via a printed circuit
30 board plugged into the ISA slot on a PC motherboard, as is known in the art. This printed circuit board is a Waters product called a BusLACE. The BusLACE digitizes the signals and communicates with the PC. The IEEE-488 interface is implemented as a daisy-chain network so multiple detector modules and instruments can plug into the one IEEE-488 connector on the BusLACE.

The output 22 from a third party detector 18 is assumed to be in analog form. The detector output signal is impressed on a pair of wires, enclosed within a shielded cable. The shielded cable connects to a piece of Waters electronics hardware called a SAT/IN (Satellite Input). The SAT/IN takes analog inputs from two devices and
5 digitizes the analog input signal. The output of the SAT/IN is an RS-232 line, which provides an input to the BusLACE. Thus, the BusLACE accepts two entirely different types of input, the IEEE-488 signals from Waters hardware, and the RS-232 signals from third party detectors.

The detectors 18 include refractive index (RI) detectors, light scattering (LS)
10 detectors, and viscometer (V) detectors.

The RI detector responds to the solution's refractive index. Given the output of this detector, subtracting the detector's baseline response and dividing by the refractive index increment dn/dc for the sample gives the concentration profile of the sample, c_i for the i th slice.

15 The RI detector is used to measure a peak's concentration profile. A suitably calibrated UV/Vis absorbance detector or evaporative light scattering detector (EVS) may be substituted in place of an RI detector to perform the same function. Any detector that can serve as a concentration detector may be used in place of the RI detector, and is within the scope of the invention. An example RI detector is the
20 detector incorporated in a Waters 150CV+ GPC Viscometry Chromatography System from Waters Corporation.

The LS detector responds to the sample by scattering light. Subtracting the detector's baseline response and applying a detector calibration procedure gives the excess Rayleigh ratio due to the sample, R_i , for each slice. An example LS detector is a
25 miniDAWN three angle laser light scattering detector from Wyatt Technology Corp. of Santa Barbara, CA.

The viscometer (V) detector responds to the sample plus solvent's viscosity. Subtracting the detector's baseline response, and dividing by the viscosity of the baseline gives the specific viscosity of the sample, sp,i , for each slice. An example V
30 detector is the detector incorporated in a Waters 150CV+ GPC Viscometry Chromatography System from Waters Corporation.

The LS and V detectors are commonly referred to as "molecular-weight sensitive" detectors, in that the detector's response is in proportion to the sample's concentration multiplied by some function of the sample's molecular weight. In the

case of light-scattering, the LS detector responds to the product of concentration and molecular weight. In the case of viscometric (V) detection, the viscometer responds to the concentration multiplied by the molecular weight raised to a power of .

Thus, for each slice, the detectors give the concentration c_i , excess Rayleigh ratio R_i , and specific viscosity sp,i for that slice.

A polymeric sample 14 contains a distribution of chain lengths. This sample's MWD can be described by the relative mass (or concentration) per unit interval of molecular weight. Because of the kinetics governing the synthesis of polymers, these distributions are conventionally described by the relative mass per unit of the logarithm of MW, as illustrated in Fig. 3. The horizontal axis is log MW and the vertical axis is arbitrary. As described, a narrow, but finite, interval in log MW of the distribution is referred to as a slice.

For explanatory purposes, the simulated MWD 35 shown in Fig. 3 will be used. Given a mass injected on column, this profile is normalized to give $dm/d\log M$, the mass per unit logarithmic interval of MW.

Fig. 5 plots the column set's molecular weight calibration curve, which is the log of the MW versus elution volume. The x-axis in Fig. 5 is elution volume, and the y-axis is log MW. The asymptotes reflect at the high molecular weight end V_o , the total excluded volume, and at the low molecular weight end V_t , the total column volume.

This line has asymptotes at high and low MW reflecting the limits on the column set by the pore size distribution. The asymptotes reflect at the high molecular weight end V_o , the volume excluded by the beads; at the low molecular weight end the asymptote is at V_t , the total column volume. Ideally, between V_o and V_t there is an elution region where a plot of log MW versus elution volume is nearly linear. This calibration curve is sample-dependent, and it also depends upon the choice of solvent, columns, and temperature.

The column calibration of Fig. 5 applied to the MWD gives the concentration of the sample versus elution volume as it elutes from the column set 39, or $c(V)$, plotted in Fig. 6. The x-axis is elution volume; the y-axis is concentration.

Each polymeric sample possesses a refractive index increment described by dn/dc , the change in the solution's refractive index per unit change of sample concentration. Multiplying the concentration profile by the refractive index increment, dn/dc , gives refractive index versus elution volume plot 40 in Fig. 7. This is a simulation of the RI detector response.

The excess Rayleigh ratio describes the fraction of incident light scattered by a polymer chain, when the wavelength λ of the incident light is comparable to or larger than the size of the chain. Assume an incident beam of unpolarized light of intensity I_o , low sample concentration c , low scattering angle θ , and small particle size. Assume
 5 that the sample in a unit volume of solution scatters the light into direction θ with respect to the beam. That part of the intensity of the light that scattered by the sample $I(\theta)$ and received at distance r is given by

$$\text{Eq. (1)} \quad \frac{I(\theta)}{I_o} = \frac{K^* (1 + \cos^2 \theta) c M}{r^2}$$

where K^* is the optical constant expressed in terms of numerical and physical
 10 constants, as

$$\text{Eq. (2)} \quad K^* = \frac{2\pi}{N_A} \left(n_o \frac{dn}{dc} \right)^2 \frac{1}{\lambda^4},$$

where N_A is Avogadro's number, and n_o is the refractive index of the solvent.

The excess Rayleigh's ratio, defined to be independent of instrumental geometry, is given by

$$\text{Eq. (3)} \quad R \equiv \frac{I(\theta)}{I_o} \frac{r^2}{(1 + \cos^2 \theta)}$$

Thus, at small angles, for slice i Eq. (1) becomes

$$\text{Eq. (4)} \quad R_i = c_i M_i K^*$$

so that the excess Rayleigh ratio is simply the product of the slice's concentration c_i ,
 20 molecular weight M_i , and the optical constant K^* .

The excess Rayleigh ratio versus elution volume 42 is also illustrated in Fig. 7. The Rayleigh ratio is obtained by multiplying each slice in the concentration profile in Fig. 6 by $M_i K^*$. This is the simulation of the profile measured by the LS detector.

The specific viscosity sp is the fractional increase in viscosity due to the
 25 presence of a sample in a viscometer. At constant flow rate, the pressure drop across a capillary tube P is proportional to the viscosity of the liquid flowing through the tube. If P_o is the pressure drop due to the solvent alone, then the specific viscosity sp of a slice containing a polymer in solution is defined as

Eq. (5)
$$\eta_{sp} \equiv \frac{P - P_0}{P_0},$$

where P is the pressure drop due to the polymer-plus-solvent solution. This expression shows that sp measures the increase in viscosity caused by the addition of the polymer to the solvent.

- 5 Each slice has an intrinsic viscosity $[\eta]$. The intrinsic viscosity (IV) is defined as ratio of the slice's specific viscosity sp divided by its concentration, c , in the limit of low concentration.

Eq. (6)
$$[\eta] = \lim_{c \rightarrow 0} \frac{\eta_{sp}}{c}$$

- 10 In GPC separations, the concentrations are low enough that the intrinsic viscosity for a slice is taken to be the slice ratio as follows:

Eq. (7)
$$[\eta]_i \equiv \frac{\eta_{sp,i}}{c_i}.$$

- The intrinsic viscosity of a polymer varies with its molecular weight. The intrinsic viscosity law (IVL) describes the dependence of the logarithm of the sample's
15 intrinsic viscosity on the logarithm of its molecular weight.

For unbranched polymers, the logarithm of the IV in general is proportional to the logarithm of the chain's molecular weight. The empirical Mark-Houwink intrinsic viscosity law expresses this linear relationship as

Eq. (8)
$$\log[\eta]_i = \log K + \alpha \log M_i$$

- 20 which is parameterized by the Mark-Houwink constants, K and α .

- Polymers can be branched. Zimm and Stockmeyer developed a physical model of long-chain, branched polymers, described in Zimm, B. and Stockmeyer, W., 1949, *J. Chem. Phys.* 17, 1301-1314, which is incorporated herein by reference. Starting from this work, a model is developed describing the intrinsic viscosity for polymers with
25 long-chain branching, which is called the Zimm-Stockmeyer (ZS) law.

In the ZS law, the distribution's intrinsic viscosity is described by four parameters, K , α , and λ .

The ZS law assumes that at low molecular weight the polymer is essentially unbranched. In this regime, the intrinsic viscosity law is asymptotically linear. The

asymptotic slope of the intrinsic viscosity law at low molecular weight is described by the Mark-Houwink constants, K and α .

At high molecular weight, when branching dominates, the asymptotic slope of the intrinsic viscosity law is less than α , and is given by $(\alpha - 1/2)$, where β is the shape factor of the polymer. Values for β are determined by the polymer/solvent system. For example, β is approximately 0.9 for a branched polyethylene in TCB. Values for β range from 0.5 to 1.5.

The molecular weight at which a polymer branches is a stochastic process described by a branching probability. The value λ is defined as the branching probability per Dalton. A typical value for λ is 0.00001 per Dalton.

The ZS law intrinsic viscosity for each slice i is a function of the molecular weight of that slice, M_i , and depends on the parameters K , α , λ and β , as follows:

$$\text{Eq. (9)} \quad \log[\eta]_i = \log K + \alpha \log M_i - \frac{\varepsilon}{2} \log \left[\frac{\lambda M_i}{c_1} + \sqrt{1 + \frac{\lambda M_i}{c_2}} \right]$$

The ZS law is implemented to describe two possible types of branched polymers, a three-branch point and a four-branch point.

The coefficients for the three-branch point are $c_1 = 9/4$, and $c_2 = 7$. The coefficients for the four-branch point are $c_1 = 3/4$, and $c_2 = 6$. Fig. 4 illustrates the Zimm-Stockmeyer IV law. Three intrinsic viscosity laws are plotted, which are Mark-Houwink law 36, Zimm-Stockmeyer law 37, and a polynomial law 38.

The third intrinsic viscosity law (polynomial) is simply an empirical description of a sample's intrinsic viscosity based on a polynomial expansion. This "law" can be regarded as an extension of the Mark-Houwink law, so that

$$\text{Eq. (10)} \quad \log[\eta]_i = \log K + \alpha_1 \log M_i + \alpha_2 \log^2 M_i + \Lambda + \alpha_N \log^N M_i$$

where N is the order of polynomial, and K and α_1 are the Mark-Houwink constants.

The specific viscosity is simulated by multiplying each slice in the concentration profile in Fig. 6 by the intrinsic viscosity law (IVL) for that slice. The IV

for that slice is obtained from the IVL, plotted in Fig. 4, curve 37. Fig. 7 plots this simulation of the specific viscosity versus elution volume plot 44 that would be obtained from the viscometer detector.

Therefore, Fig. 7 illustrates the detector profiles based on the instrumental responses to the concentration profile described in Fig. 6. To complete the simulation, the appropriate level of detector noise must be added to each of the simulated signals. Fig. 8 illustrates the profiles after the addition of the baseline noise to each of the detector responses. Shown are the RI 40', LS 42' and V 44' detector responses. In Fig. 7 and 8 the respective profiles have been normalized to have the same peak height for clarity in plotting.

For a given chromatographic system, containing a column set and solvent, together with a given sample, retention volume is a monotonically decreasing function of a chain's molecular weight. The plot of log MW versus elution volume is termed the molecular weight calibration for the sample.

Ideally, this curve would be universal, in the sense it would apply to all samples. Unfortunately, this curve is sample dependent (as well as dependent on the solvent and column set).

There is no *a priori* means to determine the MW calibration curve from a given column, solvent, and sample combination. In practice, the MW calibration curve must be determined by a calibration procedure employing the collected data.

The basis of MW calibration for RI-LS detection is the relationship between the Rayleigh ratio, molecular weight, and concentration for each slice. This relationship need only be considered in the limit of scattering at zero angle and low sample concentration. In this limit, the relationship between these parameters is:

$$M_i = \frac{R_i}{c_i} \frac{1}{K^*}$$

Eq. (11)

A more general Rayleigh scattering law includes the dependence of the excess Rayleigh ratio on the scattering angle, the molecule's radius of gyration, and the second Virial coefficient. The method of the present invention applies either to this simpler or to the more complete expression.

The significance of the relationship expressed by Eq. (11) is that only the RI and LS detector responses (curves 40 and 42, or, 40' and 42') are needed to obtain a sample's molecular weight calibration curve.

If detector noise were not present, so the RI and LS profiles were free of noise as in Fig. 7, the sample's MW calibration and MWD would be straightforward to obtain. Following Eq. (11), one would, for each slice i divide 42 the LS response R_i by 40 the respective RI response c_i . Dividing the resulting ratio by K^* obtains the measurement of the molecular weight M_i for that slice. The plot of $\log M_i$ versus elution volume would accurately determine the samples molecular weight calibration curve, which would correspond exactly to that plotted in Fig. 5. Combined with the concentration distribution 40 described by the RI response, the exact simulated MWD shown in Fig. 3 would be recovered.

Because detector noise is always present in the RI and LS profiles, the preceding method will give results that are acceptable only in the central region of the peak. Turning to the realistic situation depicted in Fig. 8 one divides 42' the noise-affected LS response R_i by 40' the respective noise-affected RI response c_i , for each slice i . Each slice-ratio is divided by K^* and the plot of $\log M_i$ versus elution volume is plotted as 46 in Figure 9.

Thus, Fig. 9 illustrates the molecular weight calibration curve 46 obtained from the RI-LS slice data of Fig. 8 through the straightforward application of Eq. (11). Clearly, the presence of noise affects this estimate of $\log M$, which fluctuates with high amplitude in the tail regions of the peak.

It would be an obvious mistake to use these slice-determined numbers directly as estimates of MW in the tails of the distribution. For example, the molecular weight calibration must be monotonically decreasing as elution volume increases.

In the prior art, to estimate the MWD, the strategy employed is to first form the logarithm of the ratio $\log M_i = \log (R_i / (K^* c_i))$ for each slice. The second step is to fit a low-order polynomial-curve to $\log M_i$ versus elution volume. It is assumed that a fitted low-order polynomial will accurately describe to the MW calibration of the column set for this separation. Other smooth curves, other than a low-order polynomial can be employed.

In the prior art, the least-squares fitting procedure can be expressed as follows:

$$\chi^2 = \sum_{i=1}^N \left(\log \left(\frac{R_i}{c_i} \frac{1}{K^*} \right) - F_i(P_0, K, P_M) \right)^2$$

Eq. (12)

where the left term on the right hand side is the molecular weight inferred for each slice
 5 from the combination of the RI and LS detector responses. The term on the right is the
 polynomial model which is used as an example, whose shape is specified by parameter
 values, P_0, \dots, P_M ,
 where

$$F_i(P_0, K, P_M) = \sum_{j=0}^M P_j i^j$$

Eq. (13)

10

and the values i are indices of the elution volume slices. The function $F_i(P_0, \dots, P_M)$ is
 the logarithm of the molecular weight for slice i . Thus $\log M_i = F_i(P_0, \dots, P_M)$, and this
 relationship describes the molecular weight calibration curve as a function of slice i .

The symbol M is used in two senses herein. When referring to a slice, M or M_i ,
 15 will stand for molecular weight. But when referring to a polynomial model curve, M
 will be the highest order exponent in the expansion and the model curve will be
 specified by $M+1$ adjustable parameters, P_0, \dots, P_M . When referring to a general model
 curve, M will be the maximum number of adjustable parameters needed to specify that
 model curve, which will then be parameterized by P_1, \dots, P_M . The symbol P , will stand
 20 for the set of parameters P_0, \dots, P_M or P_1, \dots, P_M depending on the context.

The function $F_i(P_0, \dots, P_M)$ is expressed as a function of the independent slice
 index i . One could equivalently parameterize F in terms of values that are proportional
 to slice index, such as elution volume or elution time.

In Equation 13, the summation is carried out over slices from $i=1$ to N , where N
 25 is the number of slices. The $M+1$ parameters P_0, \dots, P_M are adjusted by a suitable
 optimization algorithm that finds those value of P_0, \dots, P_M that minimizes χ^2 . By this
 means, a least-squares solution that determines the model curve

$$F_i = \sum_{j=0}^M P_j i^j \text{ is obtained.}$$

For RI-LS detection, this formulation of least-squares fitting has three well-known problems, all of which occur in the tails of the peaks and which are due to the presence of detector noise in the R_i and c_i data. The first problem is that because of this noise, R_i or c_i can fluctuate negative in the tails, so the ratio can be negative. The
 5 logarithm is undefined for negative quantities. Second, the noise induced in the term $\log\left(\frac{R_i}{c_i} \frac{1}{K^*}\right)$ is not symmetric about the mean value, since the logarithm is not a linear function of its argument. Third, the noise induced in $\log\left(\frac{R_i}{c_i} \frac{1}{K^*}\right)$ becomes large in the peak tails.

In the prior art, these limitations have been addressed by restricting the region to
 10 which the curve $F_i = \sum_{j=0}^M P_j t^j$ is fit. The fitting region is generally chosen to span the heart of the peak. The results from this fit are then extrapolated to the tails. But extrapolation of polynomial models generally gives unreliable results. In addition, it is not clear how to specify the region for the polynomial fit, and the region which is extrapolated. The results of the fit can be very sensitive to this choice of fitting region.
 15 The method according to the invention is based on the theory of maximum likelihood, which yields optimum estimation of parameters in multi-variate models, as described in *Statistics for Physicists*, B. R. Martin, (1971), Academic Press, London and New York, pages 85-98. which is incorporated herein by reference.

Fitting a multi-variate curve to data containing stochastic noise is a common
 20 problem in the statistical analysis of data. The theory of maximum likelihood describes how to find parameters values that are unbiased and have minimum sensitivity to the noise in the data. Parts of the theory are applied to analysis of RI-LS and RI-V data as described below.

The stochastic noise in the RI, LS, and V detectors corresponds to the most
 25 common type of instrumental noise, which is additive, has zero mean, and is described by a Gaussian distribution parameterized by a standard deviation. For noise described by these statistics, estimation procedures based on weighted least-squares fitting are generally optimum.

In the weighted least-squares method according to the invention, the first step is
 30 to start with a set of data d_i where i runs from 1 to N , where N is the total number of

measurements. The data is described by the model $D_i(P_1, \dots, P_M)$, where the M parameters P describe that the model values D_i . The model values D_i derives from functions such as polynomial curve that can account for the data values d_i . Each datum d_i deviates from the model by noise that has a Gaussian distribution of zero mean and standard deviation σ_i .

The optimum (least-sensitive to noise) estimate of the parameters P is obtained by finding those parameter values that minimize the following expression for χ^2 :

$$\text{Eq. (14)} \quad \chi^2 = \sum_{i=1}^N \frac{(d_i - D_i(P_1, \dots, P_M))^2}{\sigma_i^2}$$

The quantity χ^2 is a function of difference between two sets of quantities, d and D . The quantity χ^2 is the sum of squares of the point-to-point differences between two sets of quantities, d and D . Each term in the summation is the squared difference between a value for d and a value for D , and where this difference is weighted by the square of the standard deviation σ_i .

To obtain correct parameter estimates for σ_i , only the relative noise values are important. For example, if all the terms have the same noise variance, then setting $\sigma_i = 1$ for all terms (unweighted least-squares) will still yield the correct values for the parameters.

Least-squares fitting is then implemented by finding those parameters P that minimize the quantity χ^2 . Those values of P that minimize χ^2 describe the model of D that best fits the data in a least-squares sense.

In order for least-squares fitting to be implement, an algorithm must be used to find the parameters P_1, \dots, P_M that minimize χ^2 . As in any minimization procedure, the final values for P_1, \dots, P_M will not depend on the details of the algorithm adopted to perform the minimization, as long as the minimum in χ^2 is actually found.

In general, such minimization procedures require that initial parameters values be found and that an initial value for χ^2 be computed. These parameters are then iteratively adjusted until the minimum of χ^2 is found.

In the formulations of χ^2 to be discussed below, the determination of initial parameters values can be accomplished by a variety of standard methods. Such methods include the manual estimation of values that are known to approximate the expected final parameter values; the adoption of typical values of parameters; or the

implementation of a separate algorithm that determines initial parameters values from a subset of the data to be analyzed.

In the formulations of ² to be discussed below, the subsequent iterative adjustment of the parameters can be accomplished by a variety of standard methods.

- 5 Methods that find the minimum of a function of N-variables include Newton-Raphson, Levenberg-Marquadt, simplex, gradient search, and brute force search. Such iterative adjustment procedures are described in the *Numerical Recipes in C, the Art of Scientific Computing, Second Edition*, (1992) W.H. Press, S.A. Teukolsky, W.T. Vetterling, B.P., Flannery, Univ. of Cambridge, pages 394-455, which is incorporated herein by
10 reference.

In the prior art, the least-squares fitting procedure for RI-LS data is expressed as follows:

$$\chi^2 = \sum_{i=1}^N \left(\log \left(\frac{R_i}{c_i} \frac{1}{K^*} \right) - F_i(P_0, K, P_M) \right)^2$$

Eq. (15)

- The above expression for ², being a least-squares minimization appears at first
15 glance to be based on the theory of optimum estimation. However, it is not.

In the prior art, the data model is correct, because the polynomial $F_i = \sum_{j=0}^M P_j i^j$ is generally an adequate representation of the molecular calibration curve. But the noise model is not correct.

- The measurement error in $\log \left(\frac{R_i}{c_i} \frac{1}{K^*} \right)$ is non-Gaussian and is asymmetrical
20 about zero. Also, there are no weighting factors, although the noise variance of each term is different.

In the method of the prior art, unweighted least-squares has the effect of increasing the influence of terms that contain excess noise and reducing the influence of terms that have good signal-to-noise in the estimation of parameters.

- 25 All implementations of least-squares model fitting must compare two sets of quantities. In Equation 14 the quantities that are compared are the data points d and the models of the data points D . In RI-LS detection, there are three sets of slice-dependent quantities to compare. These are the Rayleigh ratios R_i measured by the LS detector,

the concentrations c_i measured by the RI detector, and a model $F_i = \sum_{j=0}^M P_j i^j$ for the molecular weight of the slice versus elution volume.

- Two successive improvements in the formulation of a least-squares minimization will now be described. The second formulation of least-squares minimization conforms to optimum estimation theory. All formulations use the same measured data values and the same parameterized model of the data, as in the prior art, but compare different quantities in performing the least-squares fit. Comparing different quantities effects a change in the noise model.
- The first improvement removes the logarithms by exponentiating both terms in Equation 15. The least-squares comparison is then modified to become,

$$\chi^2 = \sum_{i=1}^N \left(\frac{R_i}{c_i} \frac{1}{K^*} - 10^{F_i(P_0, K, P_M)} \right)^2$$

Eq. (17)

- This rearrangement removes the bias due to logarithm and allows negative values of R_i to be included. However, because c_i is in the denominator, small values of c_i in the peak tails will cause large fluctuations in this ratio.

The second improvement multiplies both terms by c_i to arrive at new quantities to compare:

$$\chi^2 = \sum_{i=1}^N \left(R_i - c_i K^* 10^{F_i(P_0, K, P_M)} \right)^2$$

Eq. (18)

This rearrangement allows the values for c_i to be small.

- The product of the concentration c_i , the optical constant K^* and the polynomial model F_i , are compared to the Raleigh ratio R_i . Because the errors in R_i and c_i are assumed to have zero mean and distributed as Gaussian, the error in each term on the right hand side of Eq. 18, will also be zero mean and distributed as a Gaussian.

In the formulation of Equation 18, all the profile data in the fit can be included, including points for which the measured values for R_i are consistent with zero and in

fact have negative values due to noise. This solves the problem of using data in the tails of the distribution. The above expression thus can be used to fit for data throughout the peak region, including the tails.

Being able to fit values for R_i that are near zero represents a major advantage in the fitting of RI-LS data. The inclusion of such data near zero adds information that helps constrain the model fit. The inclusion of negative going fluctuations actually provides useful information to the fit that was not used in the method of the prior art.

The model F_i in Eq. (18) is expressed as a polynomial expansion. However, the invention can incorporate any smooth, parameterized model curve in place of this polynomial expansion.

Equation 18 corresponds to unweighted least-squares. Generally, in the RI-LS system, the noise in the RI measurement is less than that of the LS measurement in the sense that the signal to noise ratio (SNR) of the peak apex in the RI profile is higher than that in the apex of the LS profile. If it is assumed that only the LS measurement is noisy and the RI measurement has essentially negligible noise, then unweighted least-squares yields the optimum, maximum likelihood estimate of the parameters P .

Fig. 10 plots $\log\left(\frac{R_i}{c_i K^*}\right)$ versus each slice number for a simulated

separation as curve 50. Superimposed on the slice data is the model $F_i = \sum_{j=0}^M P_j i^j$ computed two different ways. One is by minimizing x^2 in the least-squares formulation of Equation 18, giving curve 52. The other is by minimizing x^2 in the least-squares formulation of Equation 15, giving curve 54. Curve 56 is the true log M calibration curve that corresponds to the central portion of curve 56 plotted in Fig. 5 and is overlaid here for comparison. The curve fit produced by the illustrative method is insensitive to the noise in the distribution's tail. The curve fit produced by the method of the prior art is dominated by the noise in the distribution's tail.

The measured quantities c_i do contain noise. As noted, the least-square formulation can be generalized to include that as follows.

$$\chi^2 = \sum_{i=1}^N \frac{\left(R_i - c_i K^* 10^{F_i(P_0, K, P_M)} \right)^2}{\sigma_i^2}$$

Eq. (19)

Here i can take into account the variance from both terms as follows:

$$\sigma_i^2 = \delta_i^2 + \gamma_i^2 \left(K \cdot 10^{F_i(P_0, K, P_M)} \right)^2$$

Eq. (20)

where δ_i and γ_i are the standard deviations of the errors associated with the LS and RI detectors. The term in the bracket adjusts the relative contributions of these noise sources so they match the variance of the numerator. Here, the value for σ_i reflects the combined error in the LS and RI detectors. This formulation is exactly the one that gives the optimum estimate of the parameters P_0, \dots, P_M , and conforms to the theory of maximum likelihood.

Even if c_i contains significant noise, unweighted least-squares, Equation 18 can still be used. If unweighted least squares are used, all the data in the fit can still be included. The estimation of the parameter values will still be unbiased. The omission of a weighting function will result in somewhat increased sensitivity to the presence of detector noise in the profiles

An additional rearrangement of the quantities in Eq. (18) can be performed so the least-squares formulation compares $\left(R_i / K \cdot 10^{F_i(P_0, K, P_M)} - c_i \right)$. When the noise in the RI measurement is greater than the noise in the LS measurement, this rearrangement gives an optimum estimate of parameters P , using unweighted least-squares.

The next consideration is detection by a refractive index detector and a viscometer (RI-V). The goal of RI-V detection is to determine a sample's MWD and its IVL. These determinations both make use of the assumption of universal calibration.

To determine the sample's MWD, we must first determine the sample's molecular weight calibration curve, $\log M_i$ which is log molecular weight versus slice number or elution volume. To determine the IVL of a sample, $\log [\eta]$ versus $\log M_i$ we must first determine $\log [\eta]$, log intrinsic viscosity versus elution volume. Combining $\log [\eta]$ with $\log M_i$ gives us the sample's intrinsic viscosity law.

The viscometer determines the sample's specific viscosity, and the RI detector determines the sample's concentration at each slice. The intrinsic viscosity of a slice is the ratio of its specific viscosity to its concentration. The intrinsic viscosity is computed for each slice in a broad sample distribution as follows:

$$\text{Eq. (21)} \quad [\eta] = \eta_{sp,i} / c_i,$$

where the subscript i refers to the i th data slice, and where $[\eta]$ is the intrinsic viscosity of slice i , $\eta_{sp,i}$ is the specific viscosity, and c_i is the concentration of the slice.

In a gel permeation chromatography (GPC) separation, the separation is effected by a size-dependent, not mass-dependent, interaction between the polymer chain and the chromatographic bed. The assumption of Universal Calibration introduced by Benoit [Z. Grubisic, R. Rempp, and H. Benoit, *J. Polym. Sci., Part B*, 5, 753 (1967), which is incorporated herein by reference] is that the elution volume of a chain depends only on that chain's hydrodynamic volume. The hydrodynamic volume is defined to be the product of the molecular weight of a species times its intrinsic viscosity. Expressed in terms of slice quantities, this relation is:

$$\text{Eq. (22)} \quad H_i = M_i [\eta_i]$$

The physical significance of this definition can be appreciated by substituting the definition of intrinsic viscosity to obtain:

$$\text{Eq. (23)} \quad H = M[\eta] = M \frac{\eta_{sp}}{c} = \frac{\eta_{sp}}{\rho}$$

where ρ is the number density of the molecular species. Thus, hydrodynamic volume measures the viscosity per chain, in contrast to intrinsic viscosity, which measures viscosity per unit concentration.

The hydrodynamic volume for each slice is obtained by the use of narrow polymer standards of known molecular weight. RI-V detection determines the hydrodynamic volume for each standard. The standard's hydrodynamic volumes versus elution volumes can be plotted, and polynomial curves are fitted to this data to determine the hydrodynamic volume calibration curve. This curve gives the hydrodynamic volume of the column for each slice or elution volume spanned by the narrow standards. This curve is referred to either as the universal calibration of the column set, or as the hydrodynamic volume calibration curve.

The assumption of universal calibration leads to a method of calculating the absolute molecular weight distribution of a sample distribution using the responses obtained from the viscometer and RI detector. Given the hydrodynamic volume for each slice from the universal calibration curve, and the value of intrinsic viscosity obtained from each slice, we can simply compute the molecular weight of each slice from the definition

$$M_i = \frac{H_i}{[\eta]_i}$$

Eq. (24)

The straight forward application of Equations 21 and 24 to determine $\log [\eta]_i$ and $\log M_i$ is only possible for that portion of the peak centered on the peaks apex. As in
 5 the case of light scattering, the noise in these quantities increases dramatically in the peak's tails, because the quantities $\log [\eta]_i$ and $\log M_i$ both depends on the quantity $\log (sp, i/c_i)$, which requires taking the logarithm of noise-affected detector responses.

In particular, the computation of molecular weight from the ratio of Equation 24
 will usually not produce physically meaningful values in the tails of the distribution.
 10 That is, values for molecular weight computed from slice ratios will not monotonically decrease with increasing elution volume. Near the start and end-points of the profiles, they can be computed to be negative due to the influence of detector noise in the computation of $[\eta]_i$ for each slice.

However, both $\log M_i$ and $\log [\eta]_i$ need to be measured over the whole peak
 15 region, including the peak tails. Again, as in the case of RI-LS, this is typically accomplished by fitting a smooth, parameterized model to $\log M_i$ and $\log [\eta]_i$ as a function of a slice number or of elution volume. Since the quantities $\log M_i$ and $\log [\eta]_i$ both tend to be nearly linear functions of elution volume, low-order polynomials as a function of elution are typically fit to these quantities.

20 How the data analysis of the prior art practice determines a model curve for the log of the intrinsic viscosities as measured for each slice versus elution volume will now be described. An expression of the following form is used:

$$\chi^2 = \sum_{i=1}^N \left(\log \left(\frac{\eta_{sp,i}}{c_i} \right) - \log [\eta]_i \right)^2$$

Eq. (25)

where $\log [\eta]_i$ is a model curve describing the intrinsic viscosity as a function of slice i ,
 25 and the M parameters P_0, \dots, P_M such that

$$\log [\eta]_i = \log [\eta(i; P_0, K, P_M)]$$

Eq. (26)

The parameters P_0, \dots, P_M are adjusted to minimize the value for χ^2 . Typically the form
 30 for $\log [\eta]_i = \log [(P_0, \dots, P_M)]$ is a low order polynomial, such that

$$\log[\eta(i; P_0, K, P_M)] = \sum_{j=0}^M P_j i^j$$

Eq. (27)

However, the invention can incorporate any smooth, parameterized model curve in place of this polynomial expansion.

Each term in the summation is the comparison between the log of the slice values and the intrinsic viscosity obtained from the model curve. This minimization obtains the estimates of the parameters describing the intrinsic viscosity versus slice number or elution volume.

In fitting this model curve, the same issues are faced as were dealt with in the RI-LS analysis. Again a low-order polynomial is fitted to the logarithm of the ratio of noise-affected detector responses. The noise in $\log(sp/ci)$ increases dramatically in the tails, and the logarithm of negative quantities is not defined. Because of the influence of detector noise in the tails, this method can only be applied to the heart of the peak. It is up to the user to decide the demarcation between the region to which the model is fit. In the prior art the intrinsic viscosity law in the peak tails is obtained by extrapolation from this model.

In the embodiment for finding the intrinsic viscosity versus slice number, the present invention reformulates the least-squares minimization by fitting a model of specific viscosity as a function of slice number or elution value to the measured values of specific viscosity for each slice. Thus, the 2 quantity to be minimized is:

$$\chi^2 = \sum_{i=1}^N (\eta_{sp,i} - 10^{\log[\eta]} c_i)^2$$

Eq. (28)

Again the model for the IV curve is of the form of Equation 26. This expression performs a least-square minimization by comparing sp,i to the product $[\eta]ci$. Specifically, this expression compares the measured specific viscosity of each slice to the product of the measured concentrations in each slice with the model, or fit-type, for the intrinsic viscosity law, for each slice.

In arriving at this expression, the exact same logic is used in reformulating the least-squares expression as was done for light scattering. The logs are exponentiated, and each term is multiplied by ci .

If the noise in ci is minimal, the unweighted expression for in equation (28) provides an optimum estimate for parameters P_i . If the measured slice values ci contain significant noise, a preferred expression is the following,

$$\chi^2 = \sum_{i=1}^N \frac{(\eta_{sp,i} - 10^{\log[\eta]} c_i)^2}{\sigma_i^2}$$

Eq. (29)

which also conforms to the theory of maximum likelihood.

The advantages of these expressions are the same as in the case of RI-LS. The noise in the quantity $\eta_{sp,i} - [\eta] c_i$ in the numerator is nearly constant over the whole

5 peak profile. In contrast, the noise in the quantity $\log\left(\frac{\eta_{sp,i}}{c_i}\right) - \log[\eta]$ is large in the peak tails. Again, this new method can determine the intrinsic viscosity of a distribution throughout the peak—in the heart of the peak and in the peak tails.

Once the model for $\log [\eta]$ is determined, the molecular weight for each slice throughout the peak can be determined from Equation 24. For each slice, Equation 24
10 is used to express M_i as the ratio of hydrodynamic volume, as obtained from the universal calibration curve, to the intrinsic viscosity, as obtained from the model fit of the present invention, via Equations 28 or 29. Since both H_i and $[\eta]$ of Equation 24 are derived from smooth models, the resulting values for M_i will also not be significantly affected by noise in the detector's responses.

15 The present invention allows for an alternate determination of M_i from the analysis of data obtained by the RI-V system. This embodiment, again, employs a least-squares minimization that fits a model of specific viscosity as a function of slice number or elution volume to the measured values of specific viscosity for each slice. But now the model of specific viscosity depends on the slice values c_i the
20 hydrodynamic volume H_i and a model for the log molecular weight for each slice. The quantity χ^2 to be minimized is

$$\chi^2 = \sum_{i=1}^N \left(\eta_{sp,i} - \frac{H_i}{10^{\log M_i}} c_i \right)^2,$$

Eq. (30)

where, again, $\log M_i$ is described by a smooth parameterized model, which is typically a
25 low order polynomial, as follows:

$$\log M_i = \log M(i; P_0, K, P_M) = \sum_{j=0}^M P_j i^j$$

Eq. (31)

Again, the advantages of Equation 30 are the same as in the case of RI-LS. Again, as weighting function, if appropriate can be incorporated into this formulation, and these formulations are consistent with the theory of optimum estimation.

Once a model for the molecular weight versus slice number is obtained, the
5 sample's MWD can be found. Once a model for the molecular weight versus slice number is obtained, and a model for intrinsic viscosity versus slice number is found, the intrinsic viscosity law, $\log [\eta]_i$, versus $\log M_i$ is known.

Physically motivated models for intrinsic viscosity can then be fit to the model values for $\log [\eta]_i$ versus $\log M_i$. Examples of such models are the Mark-Houwink and
10 Zimm-Stockmeyer laws, Equations 8 and 9. The advantage of fitting such laws to the models values for $\log [\eta]_i$ versus $\log M_i$ is that the parameters describing those models usefully characterize the polymer sample under investigation. For example, the Mark-Houwink model can be fit to a portion of the low-molecular weight region of a branched polymer to obtain K and α for that region. The ZS model can be fit to the
15 slice values for $\log [\eta]_i$ versus $\log M_i$ over the complete peak of a branched polymer to obtain K and α for the low molecular-weight region, as well as the branching probability α and the shape factor for the polymer sample.

Even though application of the present invention produces improve values for $\log [\eta]_i$ versus $\log M_i$ as compared to methods of the prior art, the determination of the
20 physical parameters of intrinsic viscosity laws can suffer from a remaining drawback in these methods. The values for parameters that describe the intrinsic viscosity law depend upon the form of the models assumed to represent both $\log [\eta]_i$ and $\log M_i$ versus slice elution volume. If these polynomial (or other assumed) models are inaccurate in describing the true dependencies of $\log [\eta]_i$ and $\log M_i$ versus elution
25 volume, then the accuracy of parameters describing the intrinsic viscosity laws will suffer a corresponding inaccuracy.

This source of inaccuracy is not due to detector noise. Rather it arises from the errors in the form of model curves used to describe $\log [\eta]_i$ and $\log M_i$ versus elution volume. It is worth noting that these models must account for the molecular weight
30 calibration curve for the column, as well as the intrinsic character of the polymer.

The next embodiment of the present invention is directed towards determining the parameters of the intrinsic viscosity law by solving two relationships simultaneously over the whole of the data analysis region. In this method, the IV law is

determined directly from the slice data and does not require the assumption of additional ancillary models.

The two relationships to be solved are:

1. The least squares comparison of the measured specific viscosity to a prediction of the specific viscosity, which is the product of the intrinsic viscosity law model and a slice measurement of concentration. The least squares comparison is:

$$\chi^2 = \sum_{i=1}^N (\eta_{sp,i} - [\eta]_i c_i)^2$$

Eq. (32)

where χ^2 is the sum of the squares of differences computed for each slice. In this expression, the intrinsic viscosity law is a function of log molecular weight, and the form of the intrinsic viscosity is

$$\log[\eta]_i = \log[\eta(\log M_i; P_1, K, P_M)].$$

Eq. (33)

Because the MW calibration is not yet known, the minimum of this expression cannot be found without additional information. This additional information is provided by the second relationship to be solved, which is:

2. The fundamental relationship between hydrodynamic volume, intrinsic viscosity and molecular weight, for each slice i :

$$H_i = M_i [\eta]_i$$

Eq. (34)

Again, the intrinsic viscosity law is described by Equation 33.

Equation 34 is used to eliminate the dependence of M_i in Equation 33, the sample's IVL. Thus, given an explicit form of an IVL, an important part of the present invention includes re-expressing the IVL so that $[\eta]_i$ depends only on the parameters P_1, \dots, P_M and the hydrodynamic volume H_i .

This algebraic substitution will be explicitly demonstrated in the case of the linear IVL below. In the case of more complex IVLs, such as are described in Equations 9 and 10, simple algebraic substitution may not suffice to determine $[\eta]_i$ as a function of H_i in closed form. Given Equation 33, values for P_1, \dots, P_M and H_i , Equation 34 can be solved, using numerical methods, to give the value for $[\eta]_i$. These numerical methods (the solution of equations through root finding) are described in *Numerical Recipes in C, The Art of Scientific Computing, Second Edition*, (1992) W. H.

Press, S. A. Teukolsky, W. T. Vetterling, B. P. Flannery, Univ. of Cambridge, pages 347-393 which is incorporated herein by reference.

Thus, Equation 32 now depends explicitly only on the measured quantities sp,i , c_i , H_i and the parameters $P1,...,PM$. No explicit reference is made to $\log M$ in this final
 5 formation of Equation 32. Also, in contrast to the prior art, there is no reference to elution volume as an independent variable. Thus, the parameters of the IVL are determined by a single fit to the measured detector responses.

After minimization, a fitted value for $[i]$ for each slice has been obtained. From this value and the known value for H_i , M_i is determined from direct computation from
 10 the fundamental relationship $H_i \equiv M_i[\eta]$. The MWD of the sample is thereby obtained. Again, no additional fit is required.

Fig. 11 plots the IV law as determined by the prior art method which relies on extrapolation, and the IV law as determined by the illustrative method. Four curves are superposed: the IV determined from the slices 60, the IV law determined from the
 15 illustrative method of the present invention 62, the IV law determined by the method of the prior art 64, and the sample's MWD for reference 35, Fig. 3.

As in the case of light-scattering, the least-squares problem is now formulated to avoid taking ratios or logarithms of ratios of noisy data. The noise in each term is of the same magnitude so the use of unweighted least-squares is appropriate. The fit can
 20 be performed to all the baseline-corrected data in the peak region. The measured values sp,i and c_i can be near zero and contain noise that causes these responses to fluctuate about zero.

In the present invention for the formulation of ², the inclusion of measurements consistent with zero response actually improves the constraints on the parameters
 25 describing the IVLs, such as K and α . Therefore the present invention is considerably less sensitive to measurement errors, especially in the tails of the peaks.

Further, the advantage of fitting two equations simultaneously means that the IV law and molecular weight calibration are estimated from a single fit to all the slice data. Performing multiple fits and extrapolations is no longer necessary. In the prior art, the
 30 additional fit is a potential source of systematic error, as special, column-dependent fit-types might have to be assumed.

In the case where the IV law is linear, Equation 8,
 $\log[\eta] = \log K + \alpha \log M$, is re-expressed as $[\eta] = KM^\alpha$.

so the relationship between hydrodynamic volume and molecular weight is

$$H = KM^{\alpha+1}.$$

5 We can therefore eliminate M_i and express the IVL as

$$\text{Eq. (35)} \quad [\eta]_i = K^{\frac{1}{1+\alpha}} H_i^{\frac{\alpha}{1+\alpha}}.$$

The expression to be minimized is then:

$$\text{Eq. (36)} \quad \chi^2 = \sum_{i=1}^N \left(\eta_{sp,i} - K^{\frac{1}{1+\alpha}} H_i^{\frac{\alpha}{1+\alpha}} c_i \right)^2$$

In this final form, χ^2 is expressed only in terms of the measured slice values, sp,i , Hi , and ci , and the parameters K and α . No explicit reference to elution volume is made.

15 Given that the values of K and α that minimize χ^2 are found by some suitable minimization algorithm, the molecular weight of each slice is obtained from the relationship $M_i = (H_i/K)^{1/(1+\alpha)}$, and the model values for $[\eta]_i$ for slice i are obtained from Eq. (35).

20 In the illustrative embodiment, the present invention is implemented using the formulation described in Equations 8, 9 and 10, which define three fit-types for the logarithmic intrinsic viscosity law. These are a linear function of log molecular weight, a Zimm-Stockmeyer law describing long-chain branching, and a higher order polynomial function.

Fig. 12 illustrates the steps performed by an illustrative embodiment of the present invention as described in detail hereinbefore. Data 100 obtained from a first detector (for example, slice data from a concentration detector) is combined with a parameterized model curve describing the sample property 103 to construct a model curve, step 104. Data 102 is obtained from a second detector (for example, slice data from a molecular weight sensitive detector). A least-squares minimization algorithm is performed, step 108. Details of the least-squares minimization algorithm will be described below. The result is a best fit model curve and parameters, step 110.

Fig. 13 illustrates the steps for an embodiment for estimating a sample's molecular weight distribution (MWD) from RI-LS detection as described in detail hereinbefore. Data is obtained from a concentration sensitive detector (such as an RI detector) 18a. The data is processed obtaining the concentration of slices, step 105. A
 5 parameterized model describing $\log M$ versus elution volume (Eq. 13) 103a is used with the concentration slices 105 to construct a model curve describing Rayleigh Ratio of the slices by

$$c_i K^* 10^{F_i(P_0, K, P_M)}$$

Eq. (37)

10 in step 104a. Second data from a molecular weight sensitive detector (such as an LS detector) 18b is processed into slices, and the Rayleigh Ratio is determined for each slice, step 112. A least-squares minimization algorithm is performed using Eq. (18) or Eq. (19), step 108, resulting in a best fit model curve describing $\log M$ versus elution volume, as shown by curve 52 in Fig. 10. The sample's molecular weight distribution is
 15 then produced, step 120 Fig. 13.

Fig. 14 illustrates the steps for an embodiment for estimating a sample's intrinsic viscosity from RI-V detection, as described in detail hereinbefore. Data is obtained from a concentration sensitive detector (such as an RI detector) 18a. The data is processed as a concentration of slices, step 105. A parameterized model describing
 20 $\log [\eta]$ versus elution volume (Eq. 27) 103b is used with the concentration slices 105 to construct a model curve describing specific viscosity of the slices, by

$$\text{Eq. (38)} \quad c_i 10^{\log[\eta]_i}$$

25

in step 104b. Second Data from a viscosity detector 18c is processed using the specific viscosity for slices, step 116. A least-squares minimization is performed, using Eq. (28) or Eq. (29) step 108. A best-fit model of $\log [\eta]$ versus elution volume (Eq. (27)) is produced, step 110b.

30 Fig. 15 illustrates the steps performed according to another embodiment for simultaneously estimating a sample's intrinsic viscosity and molecular weight distribution from RI-V detection according to the present invention, as described in

detail hereinbefore. Data is obtained from a concentration sensitive detector (such as an RI detector) 18a. The data is processed as a concentration of slices, step 105. A parameterized model describing $\log [\eta]$ versus $\log M$ (the IVL) 103c, Eq. (33), is used with concentration slices to construct an initial model curve, step 104c. Also used to
 5 construct the model curve is hydrodynamic volume of slices from the universal calibration curve, step 119. The initial model curve produced in step 104c includes constraints describing intrinsic viscosity of slice data (Eq.(34)).

Second Data from a viscosity detector 18c is processed obtaining the specific viscosity for slices, step 116. A least-squares minimization, step 108, is performed on
 10 the constructed initial model curve 104c and the specific viscosity of slice data 116 (Eq. 32). A model curve describing $\log [\eta]$ versus $\log M$ is produced, step 110c, (Eq. 33). From this curve 110c, the model curve describing $\log M$ versus elution volume, is produced, step 110a, according to

15 Eq. 39
$$\log M_i = \log H_i - \log[\eta_i]$$

and the sample's molecular weight distribution is then produced, step 120. Finally, also from the curve 110c the model curve of $\log [\eta]$ versus elution volume is produced, step 110b.

20 Fig. 16 details the least-squares minimization step 108 of Figs. 12-15. The initial model curve 104 (produced from slice data from a concentration detector 18a) is compared with slice data 102 from a detector 18b, by computing χ^2 using the equations including Equations 18, 19, 28, 29, 30, 32 and 36. As previously described the model parameters are adjusted, step 126, and χ^2 is again computed until χ^2 has been minimized,
 25 step 124. At this point, the best fit model curve and best fit model parameter have been determined, step 110.

While specific examples of RI, V and LS detectors are described in the embodiments herein, it will be appreciated that other detectors, such as other models and/or from other manufacturers, can be implemented.

30 Although the invention has been shown and described with respect to exemplary embodiments thereof, various other changes, omissions and additions in the form and detail thereof may be made therein without departing from the spirit and scope of the invention.

What is claimed is:

1. On a computer system, a method of determining molecular weight distribution (MWD) of a sample processed using gel permeation chromatography apparatus, said
5 method comprising:
 - obtaining first data from a first detector detecting said sample;
 - obtaining an initial parameterized model curve describing sample properties;
 - constructing an initial model curve from said first data and said initial
10 parameterized model curve;
 - obtaining second data from a second detector detecting said sample;
 - determining a best fit parameterized model curve and best fit parameters, from
said initial parameterized model curve to provide a molecular weight calibration for
said chromatography apparatus; and
 - obtaining a concentration profile of said sample using said chromatography
15 apparatus, and using said molecular weight calibration and said concentration profile to
determine said MWD.
2. The method of claim 1 wherein said first detector includes a concentration
20 sensitive detector.
3. The method of claim 1 wherein said second detector includes a molecular
weight sensitive detector.
4. The method of claim 1 wherein said second detector includes a Light Scattering
25 (LS) detector.
5. On a computer system, a method of determining intrinsic viscosity versus
elution volume of a sample processed by gel permeation chromatography, said method
comprising:
30
 - obtaining first data from a first detector detecting said sample;
 - obtaining an initial parameterized model curve describing log intrinsic viscosity
versus elution volume;
 - constructing an initial model curve of specific viscosity from said first data and
said initial parameterized model curve;

obtaining second data from a second detector detecting said sample; and
determining a best fit model curve of log intrinsic viscosity versus elution
volume.

5 6. The method of claim 5 wherein said first detector includes a concentration
sensitive detector.

7. The method of claim 5 wherein said second detector includes a molecular
weight sensitive detector.

10

8. The method of claim 5 wherein said second detector includes a viscometer (V)
detector.

9. On a computer system, a method of substantially simultaneously determining
15 molecular weight distribution (MWD) and intrinsic viscosity law (IVL) of a sample
processed by gel permeation chromatography, said method comprising:

obtaining first data from a first detector detecting said sample;
obtaining an initial parameterized model curve describing log intrinsic viscosity
versus log molecular weight;

20 obtaining hydrodynamic volume of slices from a universal calibration curve;
constructing an initial model curve of specific viscosity from said first data, said
initial parameterized model curve, and said hydrodynamic volume of slices;

obtaining second data from a second detector detecting said sample;
determining IVL as a best fit model curve of log intrinsic viscosity versus log
25 molecular weight; and

obtaining molecular weight calibration information obtained from said IVL; and
determining said MWD from said molecular weight calibration information.

10. The method of claim 1 wherein said initial model curve represents a Rayleigh
30 ration of said sample versus elution volume.

11. The method of claim 1 wherein said step of obtaining said initial parameterized
model curve involves obtaining a curve that describes said molecular weight calibration
as a function of elution volume.

12. The method of claim 1 wherein said step of determining said best fit parameterized model curve and best fit parameters involves performing a least squares minimization fit on said initial model curve and said second data.
- 5
13. The method of claim 1 wherein said concentration profile is obtained using said first detector.
14. The method of claim 5 wherein said step of determining said best fit model curve of log intrinsic viscosity versus elution volume involves performing a least
- 10 square minimization fit on said initial model curve and said second data.
15. The method of claim 9 wherein said step of determining IVL as said best fit model curve of log intrinsic viscosity versus log molecular weight involves performing
- 15 a least squares
16. The method of claim 9 wherein said first detector includes a concentration sensitive detector.
- 20 17. The method of claim 9 wherein said second detector includes a molecular weight sensitive detector.
18. The method of claim 9 wherein said second detector includes a viscometer (V) detector.
- 25

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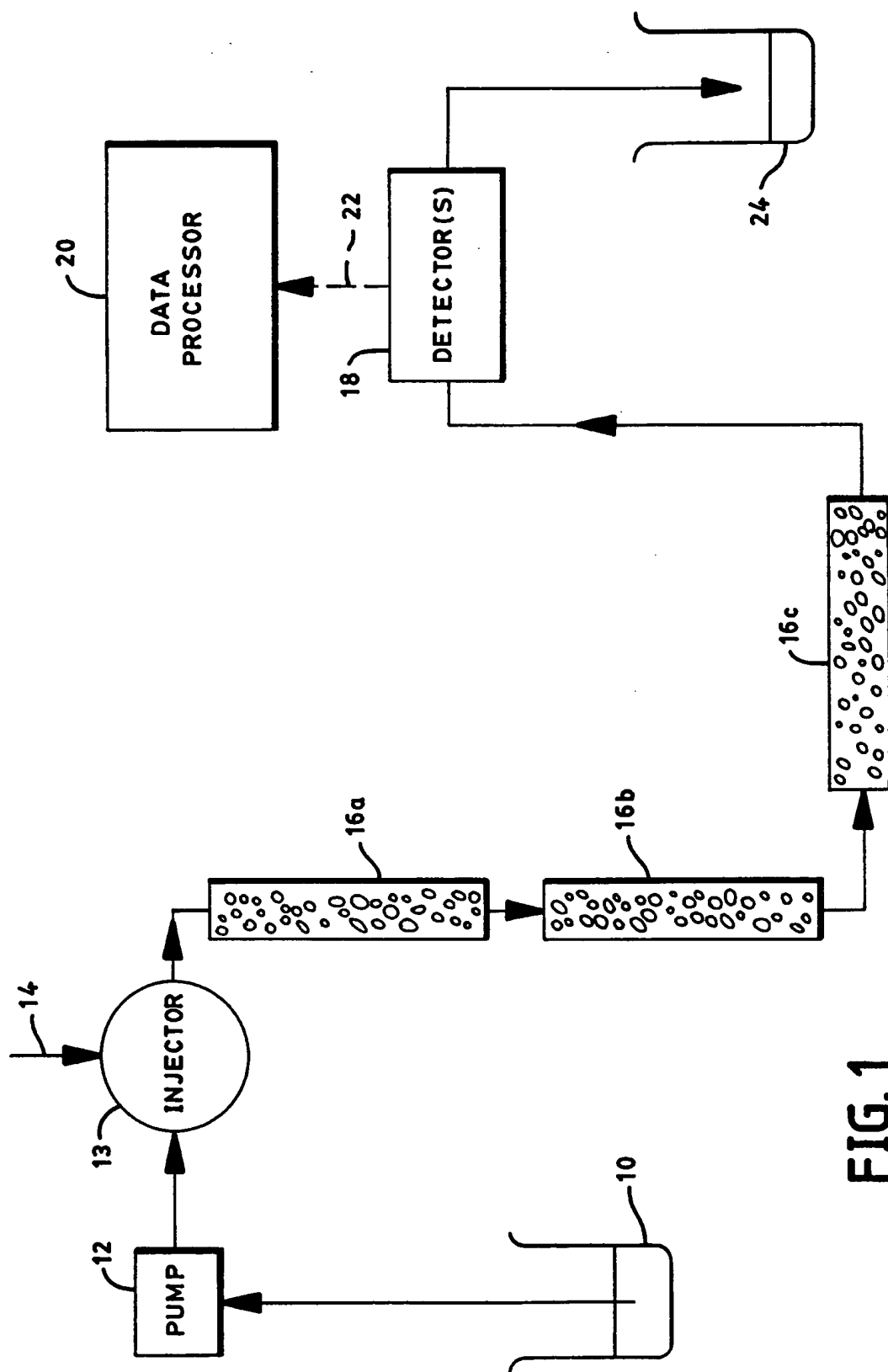


FIG. 1

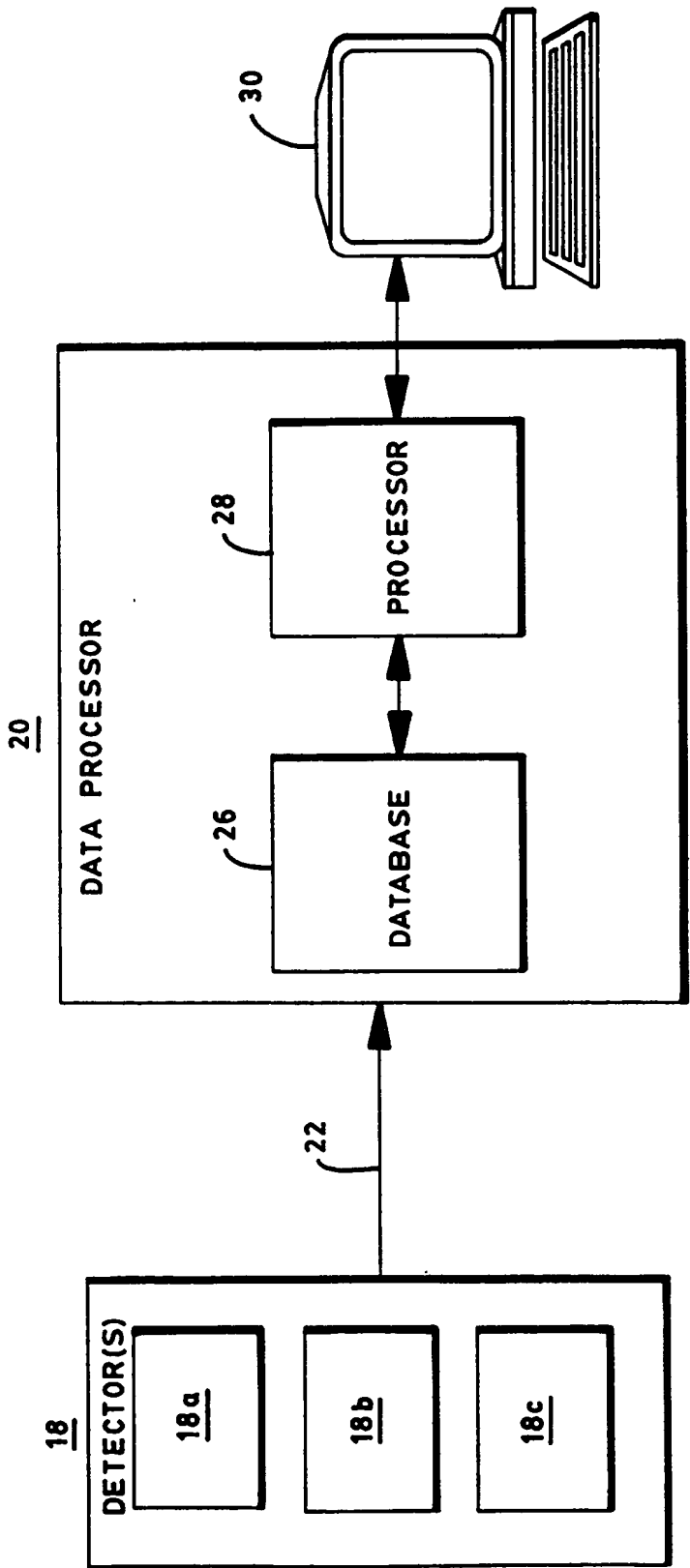
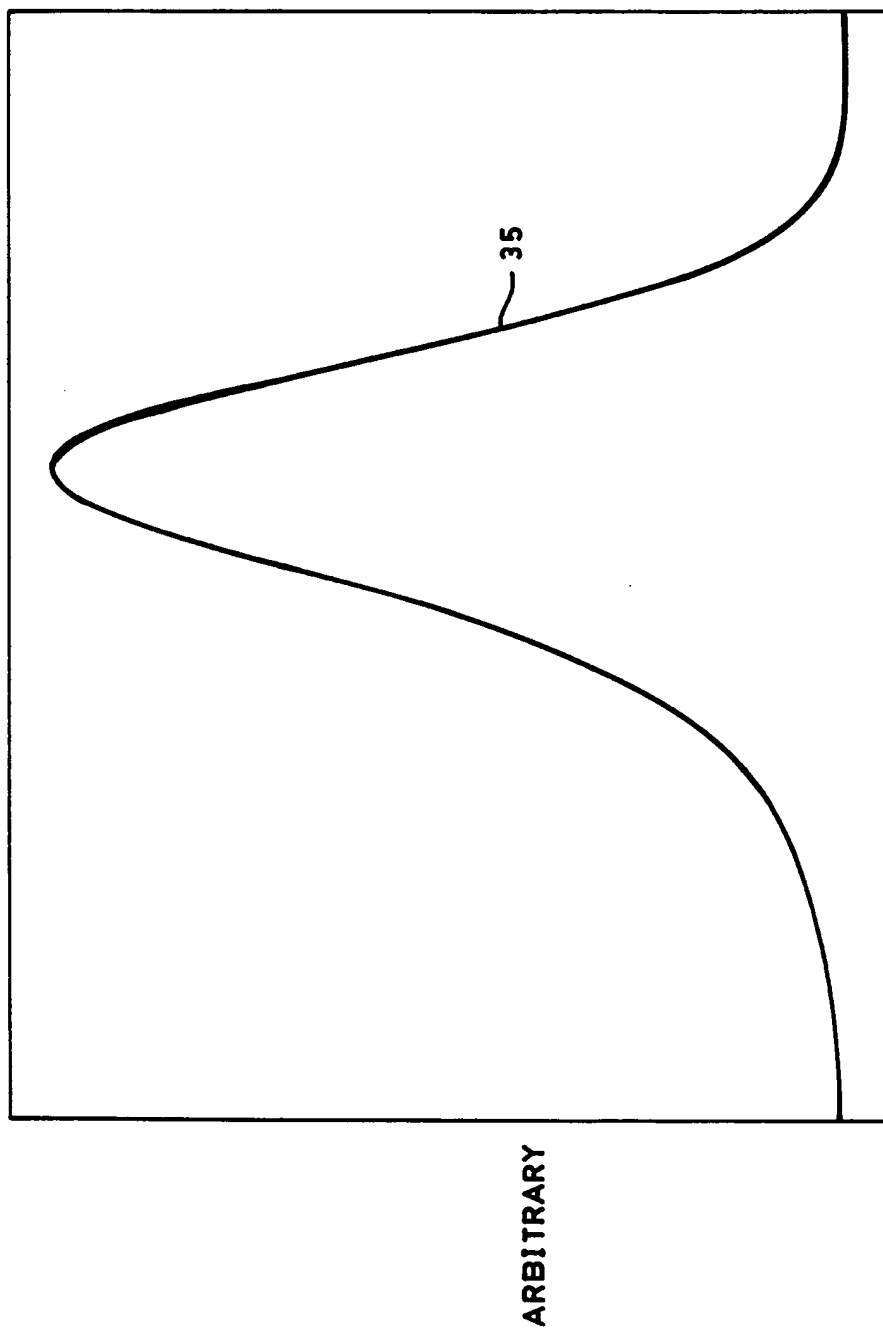


FIG. 2

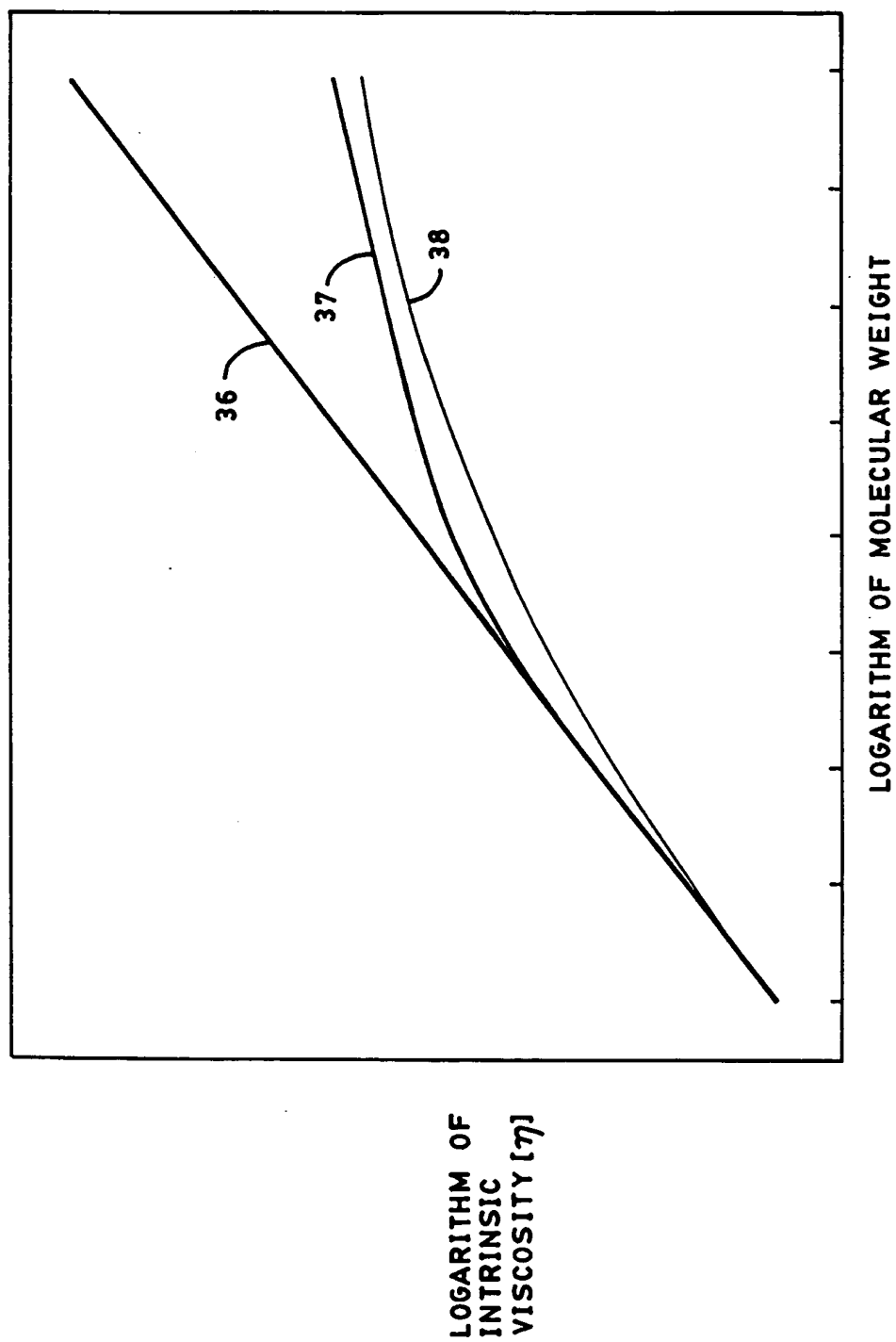
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LOGARITHM OF MOLECULAR WEIGHT

FIG. 3

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**FIG. 4**

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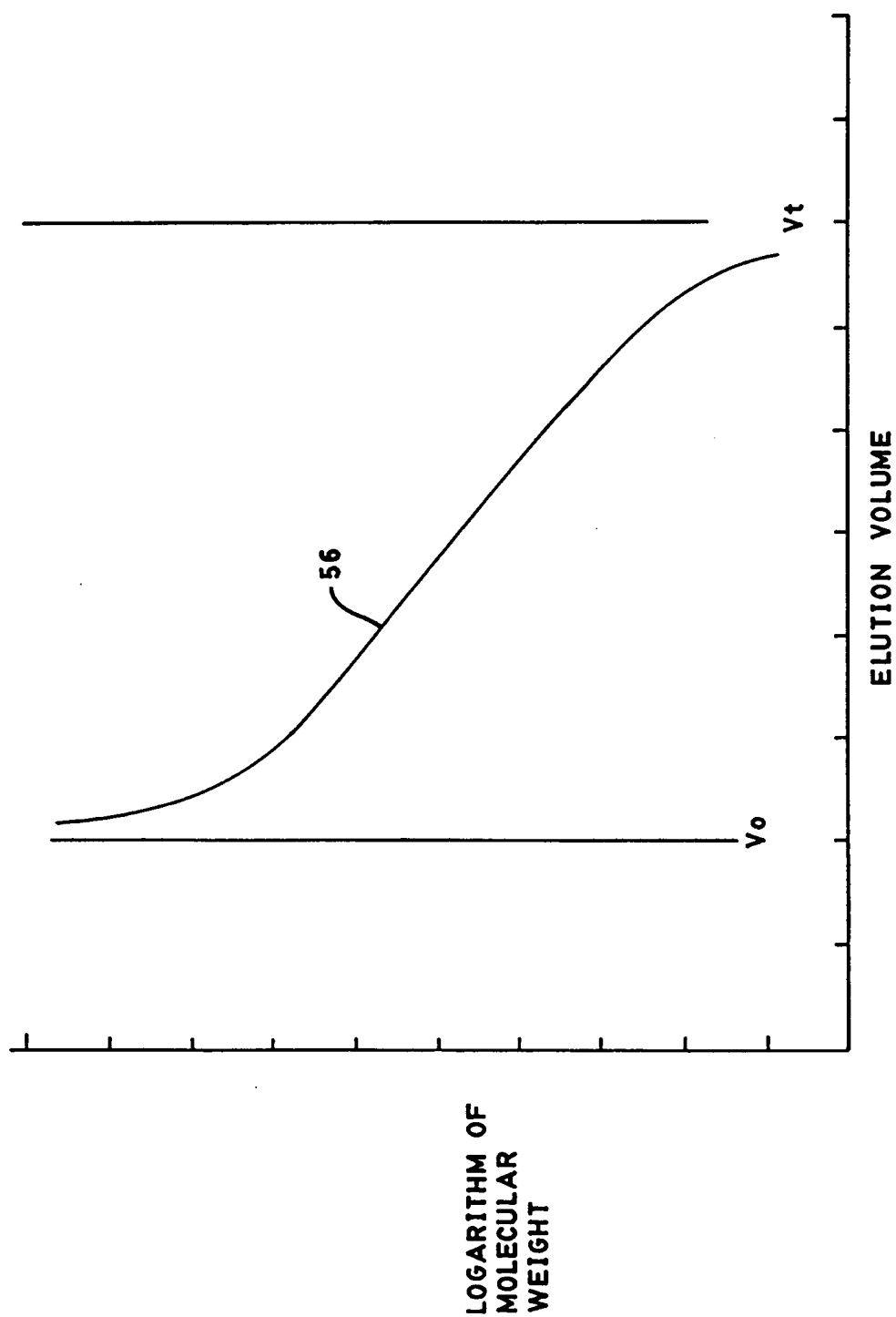
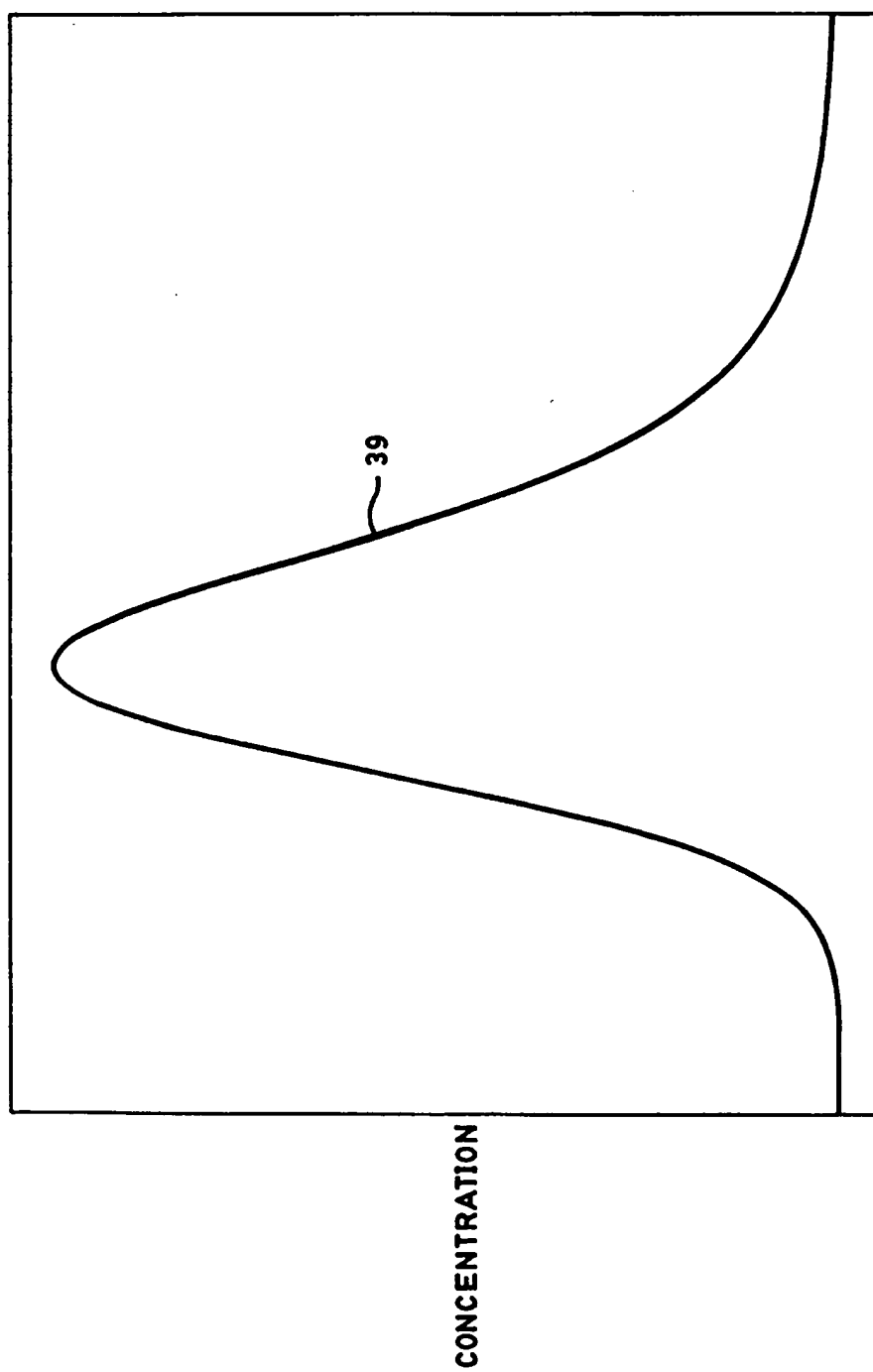


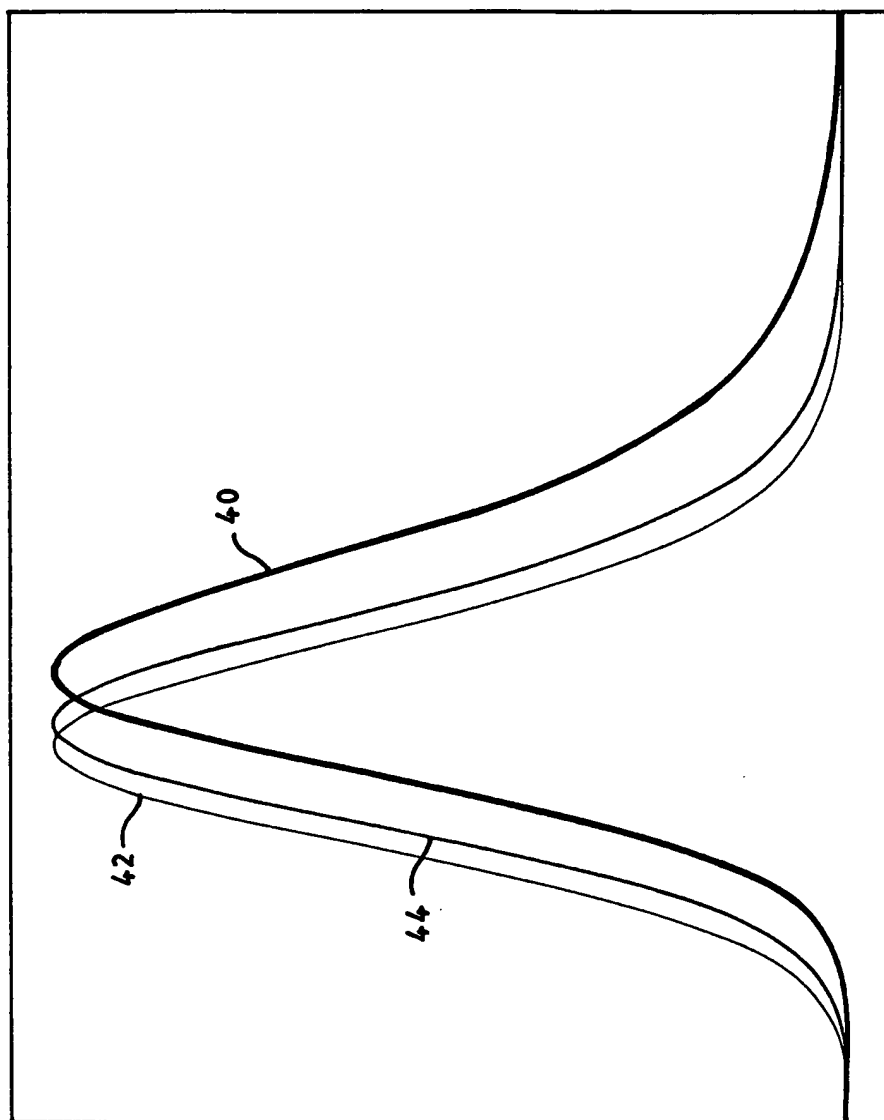
FIG. 5



ELUTION VOLUME

FIG. 6

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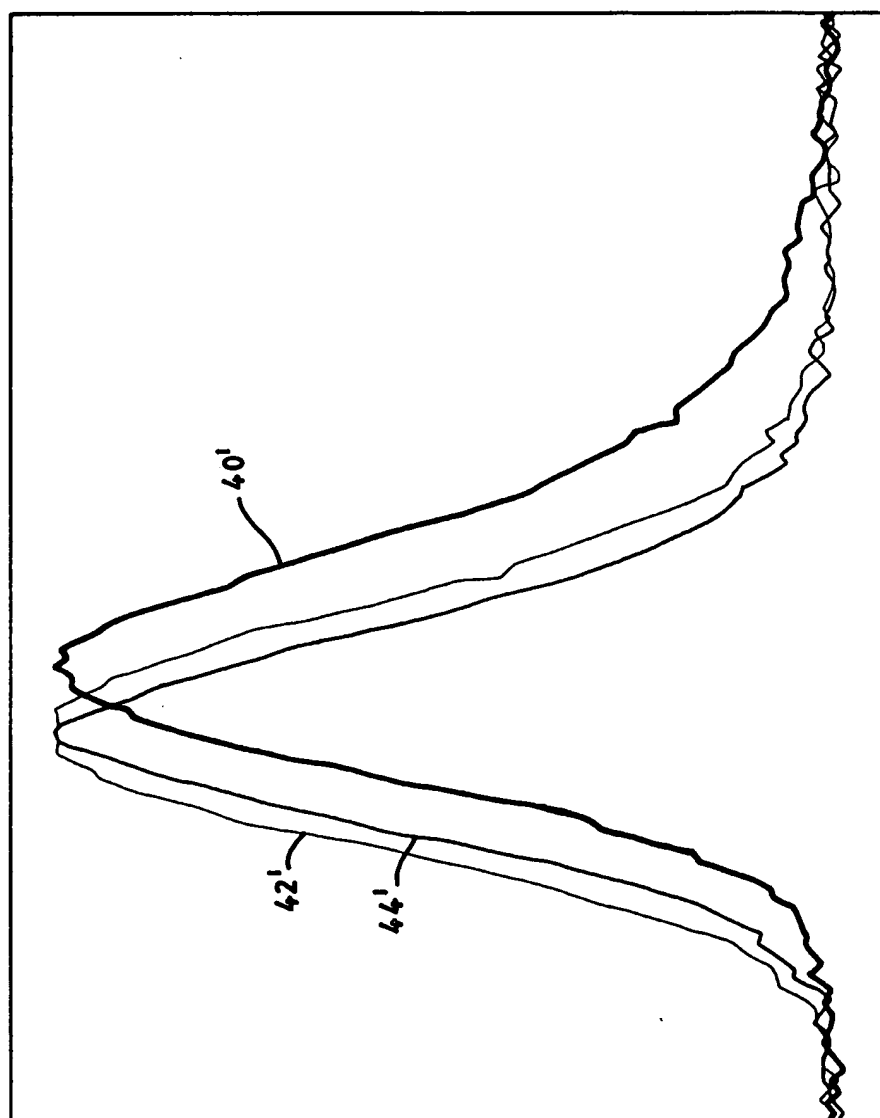


ELUTION VOLUME

FIG. 7

NORMALIZED
DETECTOR
RESPONSES

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ELUTION VOLUME

FIG. 8

NORMALIZED
DETECTOR
RESPONSES

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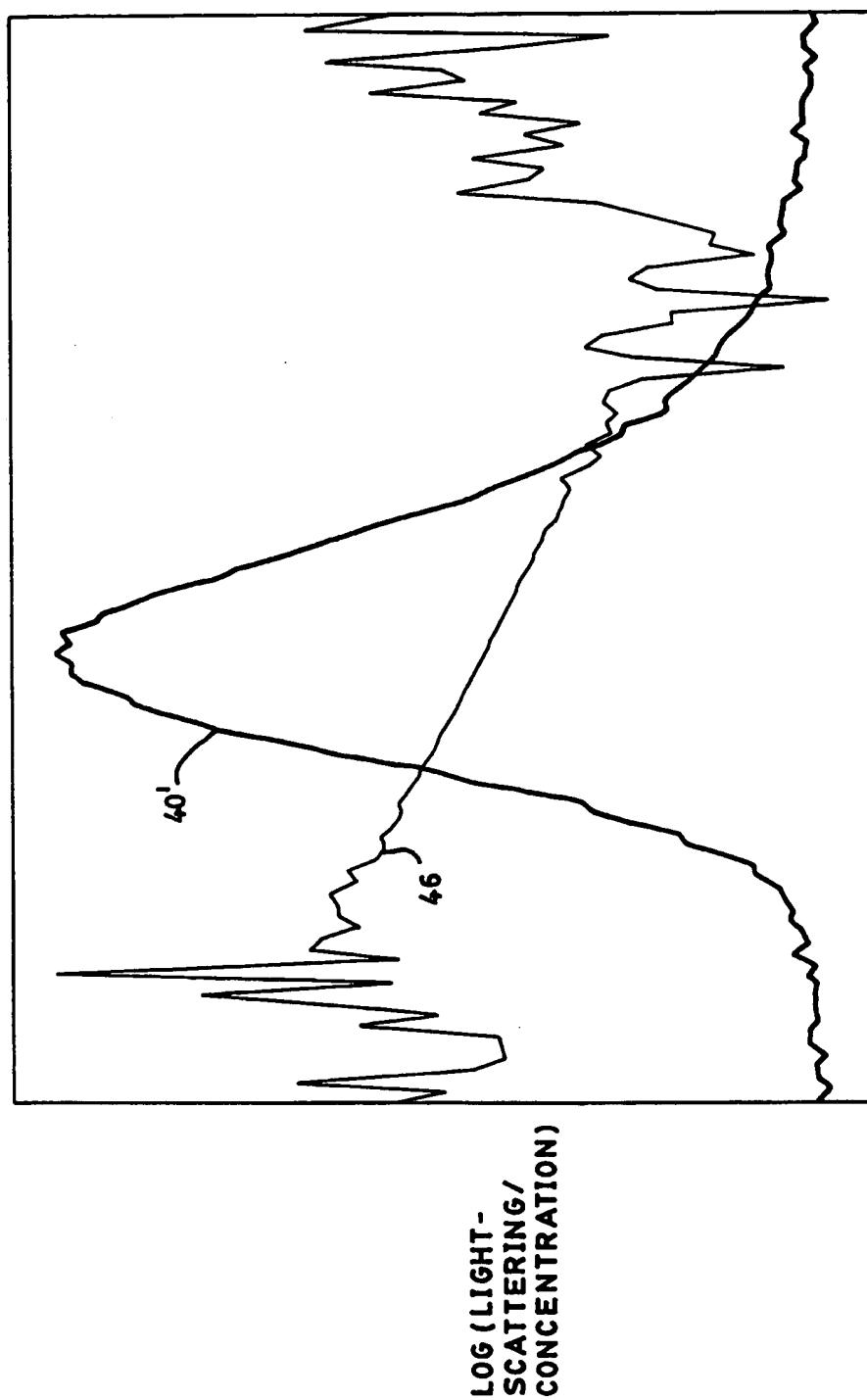
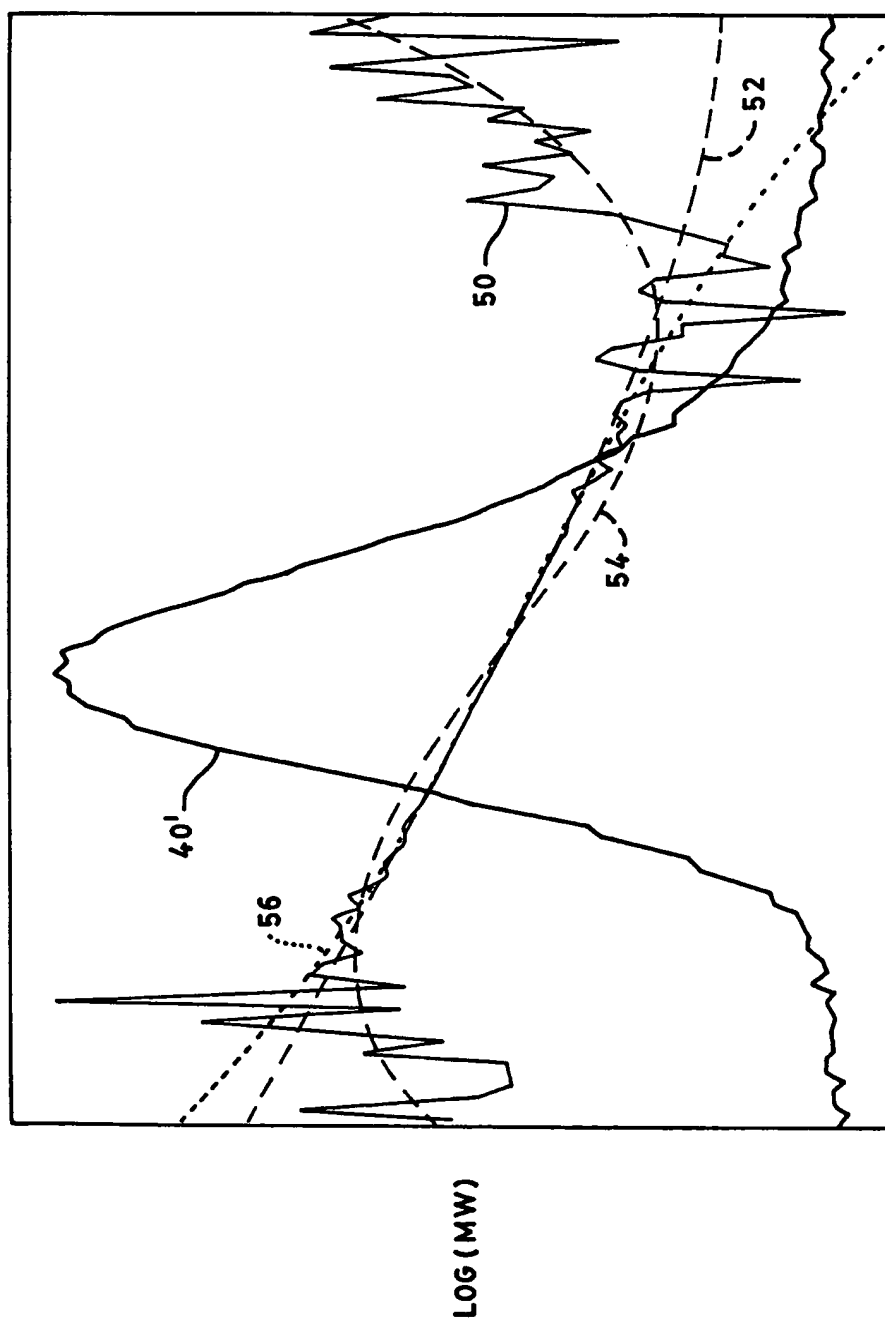


FIG. 9

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ELUTION VOLUME

FIG. 10

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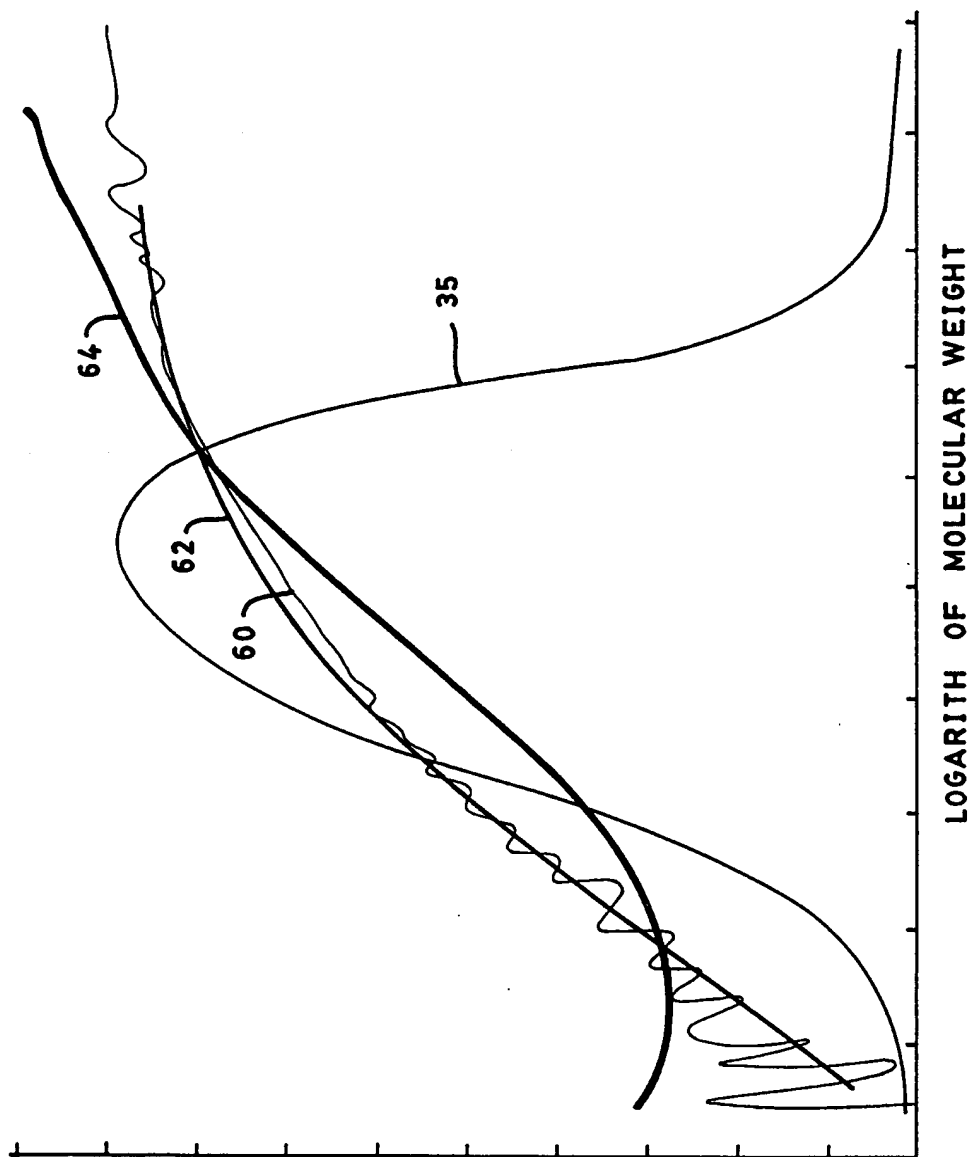


FIG. 11

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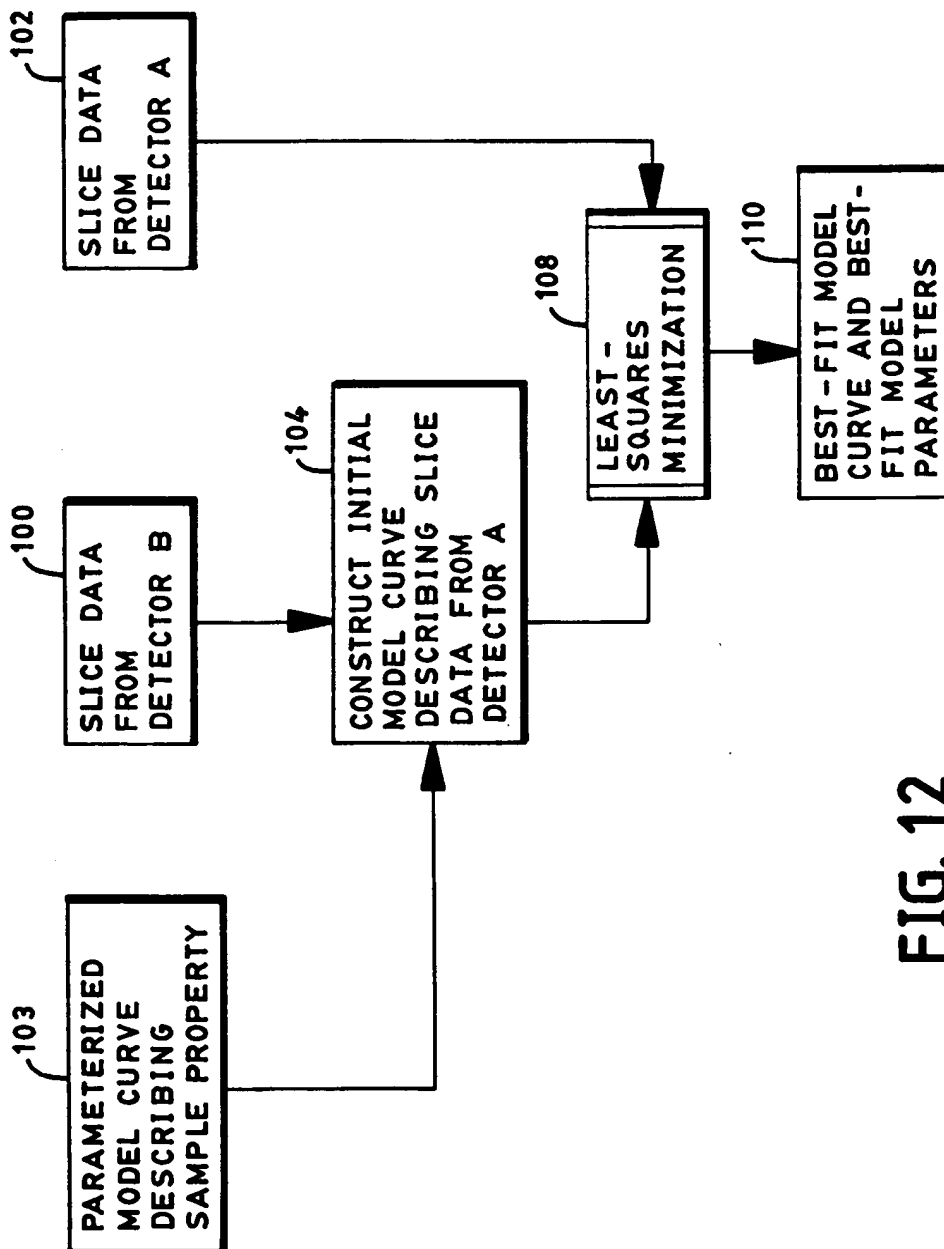


FIG. 12

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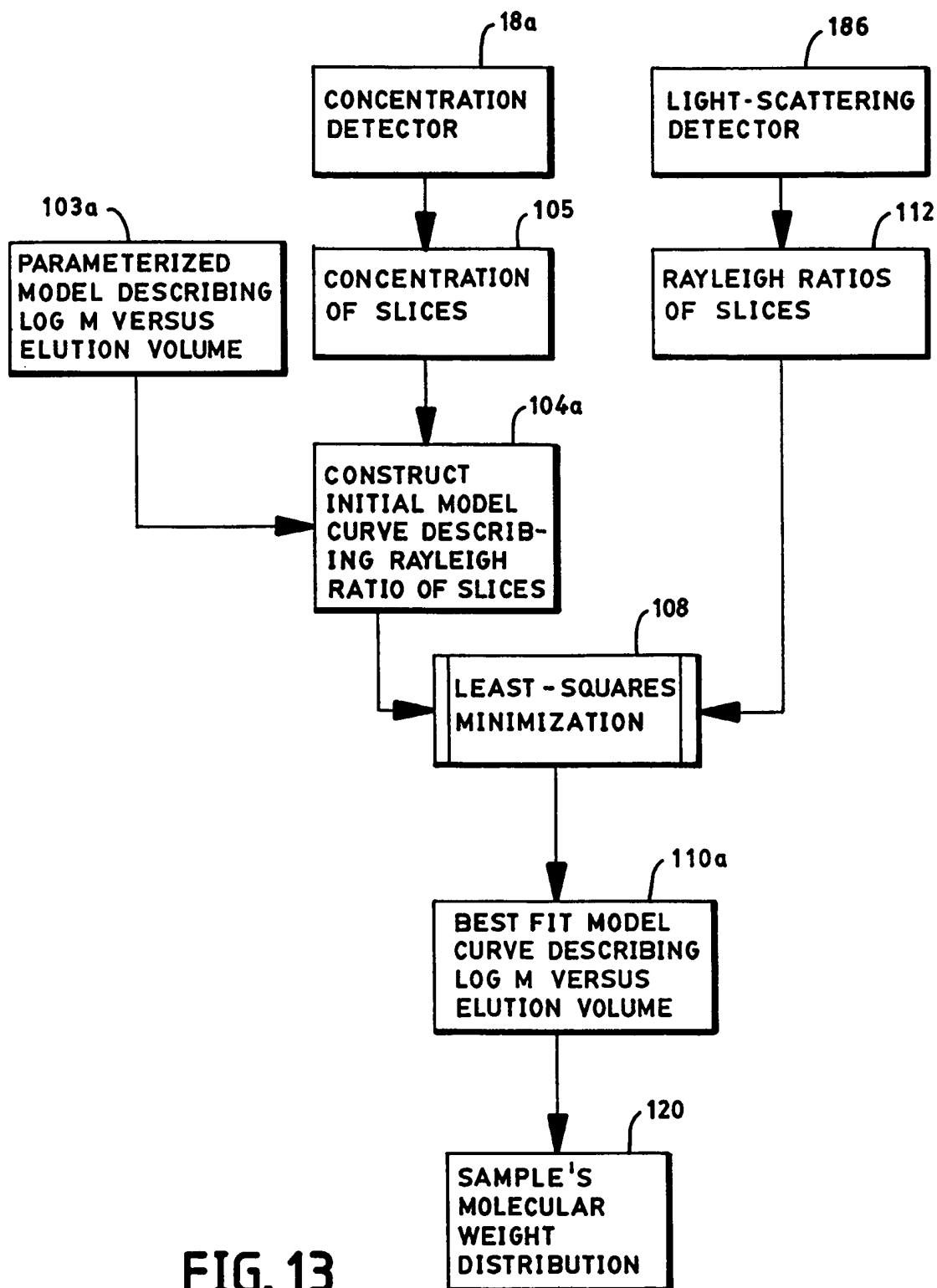


FIG. 13

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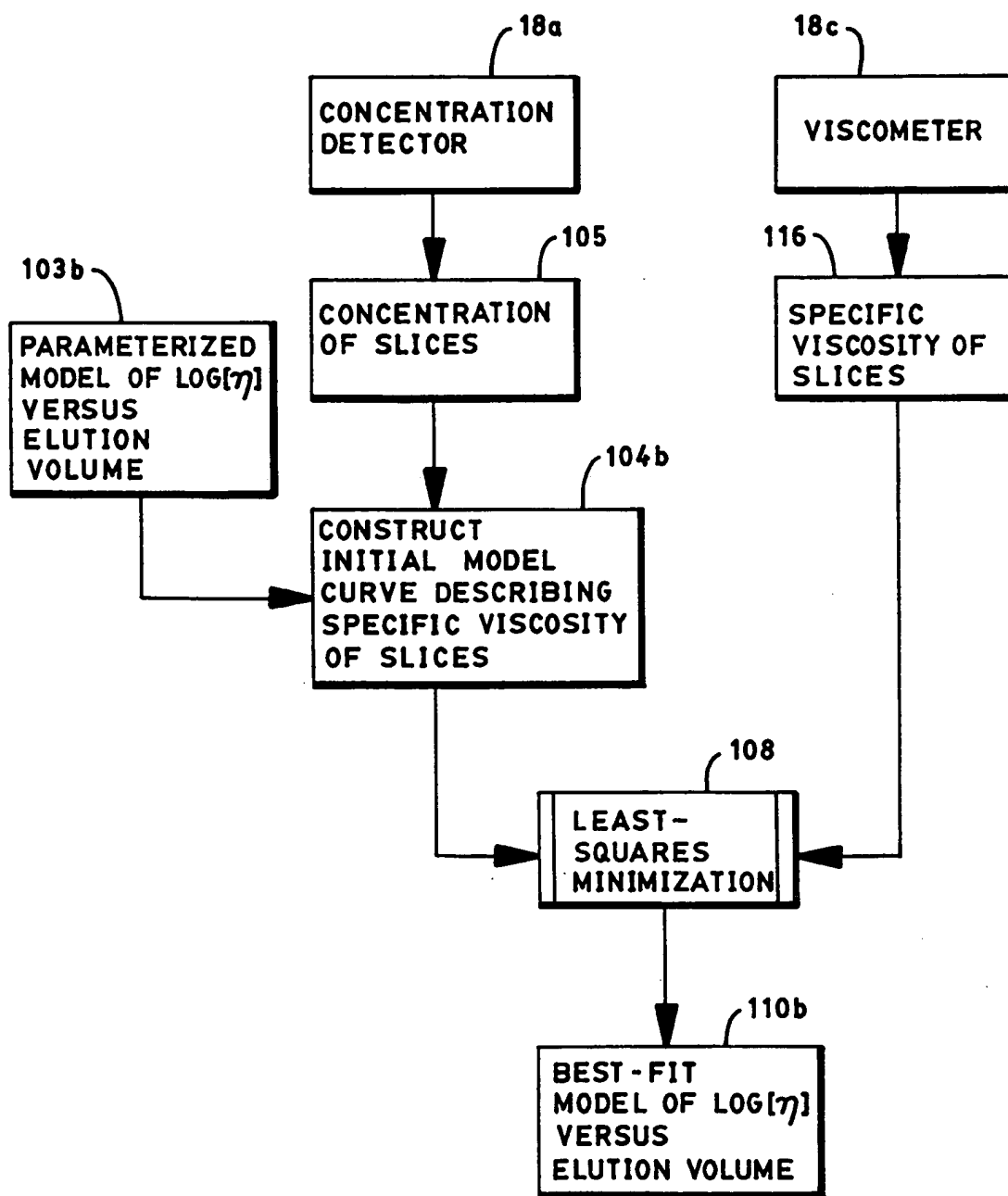


FIG. 14

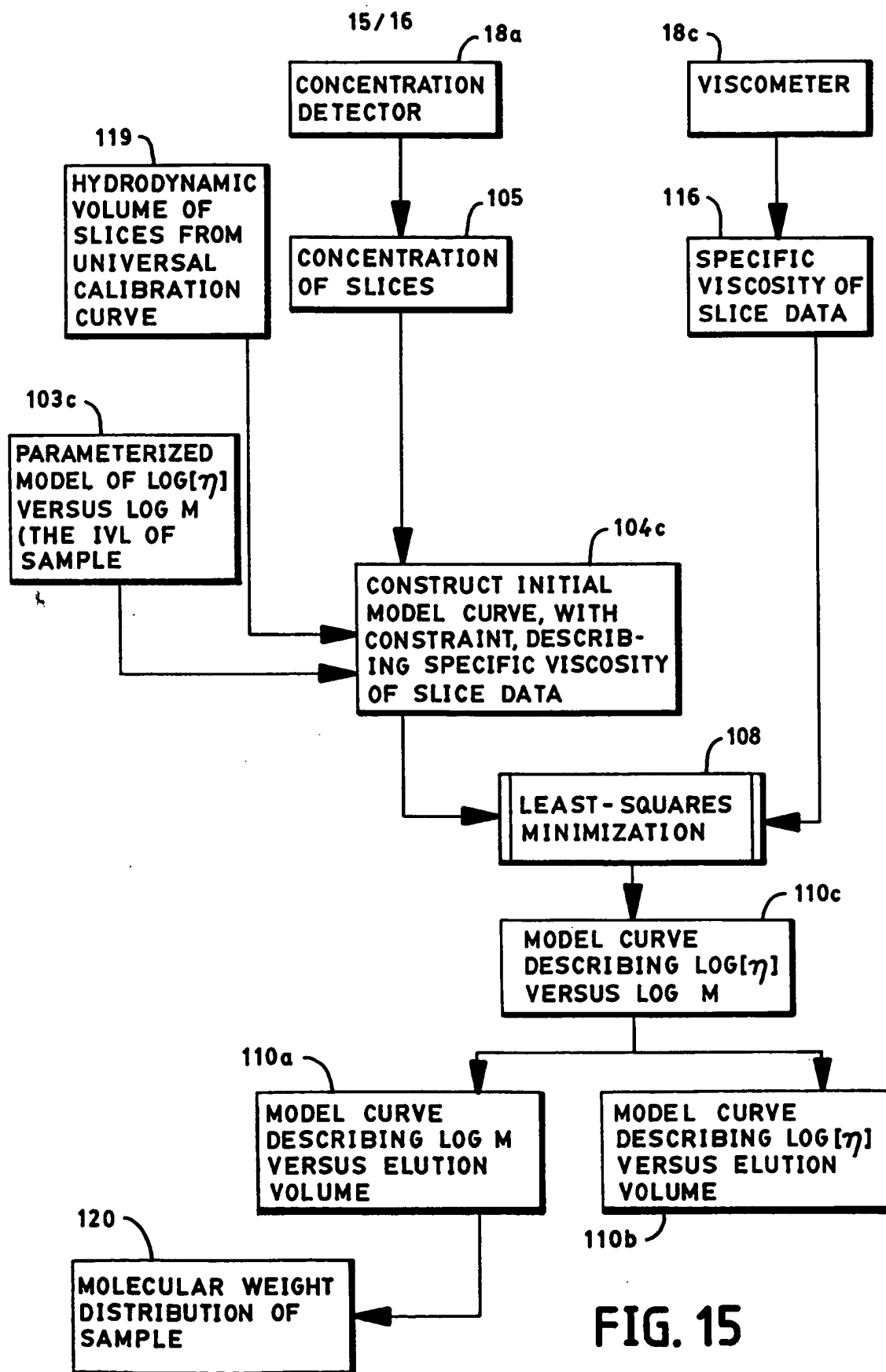


FIG. 15

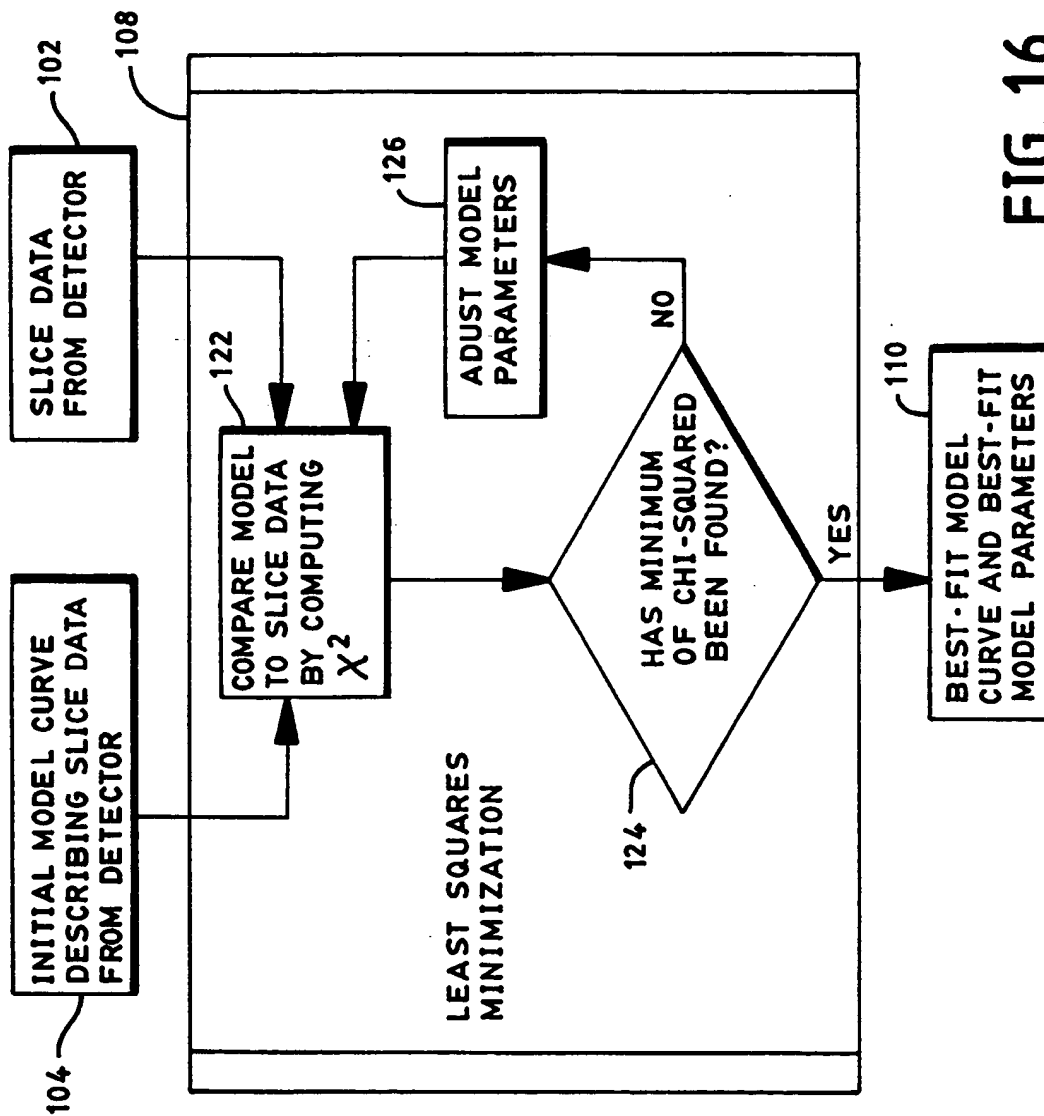


FIG. 16

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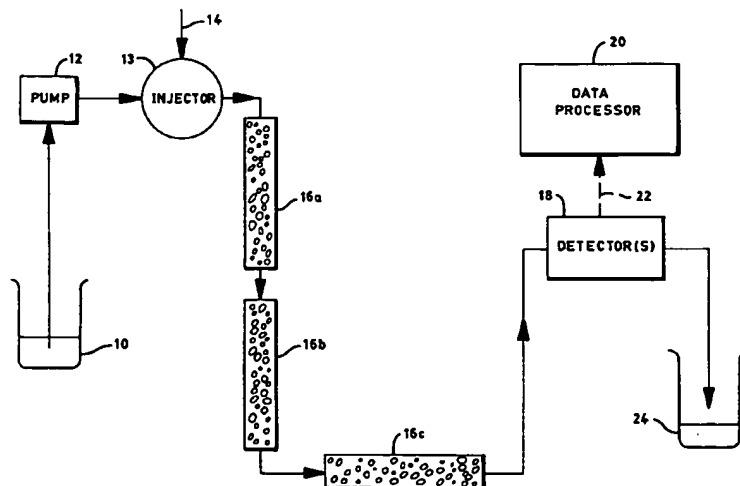
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(54) Title: **SYSTEM AND METHOD FOR DETERMINING MOLECULAR WEIGHT AND INTRINSIC VISCOSITY OF A POLYMERIC DISTRIBUTION USING GEL PERMEATION CHROMATOGRAPHY**



(57) Abstract: A system and method for analyzing data from a gel permeation chromatography (GPC) or size exclusion chromatography (SEC) system for determining a polymeric sample's molecular weight distribution (MWD) and intrinsic viscosity law (IVL). Data from two or more detectors (18) is used with a least-squares minimization fit. A novel method includes the simultaneous determination of a sample's MWD and IVL using data from two or more detectors (18). Detectors (18) include a Light Scattering (LS) detector, viscometer (V) and a refractive index (RI) detector. The present invention is insensitive to detector noise in the baseline regions of the peak curve.

INTERNATIONAL SEARCH REPORT

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Minimum documentation searched (classification system followed by classification symbols)

U.S. : 702/23, 30, 27; 73/61.52; 210/656

Documentation searched other than minimum documentation to the extent that such documents are included in the fields searched

Electronic data base consulted during the international search (name of data base and, where practicable, search terms used)
EAST - chromatography, molecular weight distribution, gel permeation, detector

C. DOCUMENTS CONSIDERED TO BE RELEVANT

Category *	Citation of document, with indication, where appropriate, of the relevant passages	Relevant to claim No.
A	US 4,775,943 A (CHAMBERLIN et al.) 04 October 1988 (04.10.1988), see entire document.	1-18
A	JACKSON et al. Molecular Weight-Sensitive Detectors for Size Exclusion Chromatography. Handbook of Size Exclusion Chromatography. 1995, Vol. 69, pages 103-145.	1-18

☒ Further documents are listed in the continuation of Box C.

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